

Understanding and Modeling Polymers: The Challenge of Multiple Scales

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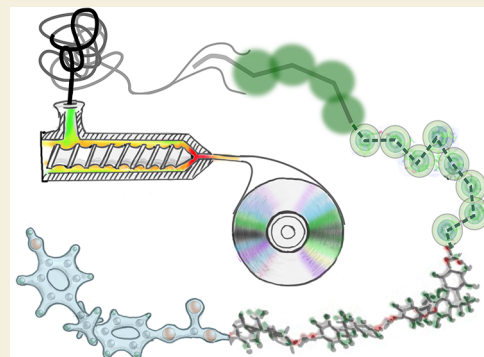
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ABSTRACT: Polymer materials are multiscale systems by definition. Already the description of a single macromolecule involves a multitude of scales, and cooperative processes in polymer assemblies are governed by their interplay. Polymers have been among the first materials for which systematic multiscale techniques were developed, yet they continue to present extraordinary challenges for modellers. In this Perspective, we review popular models that are used to describe polymers on different scales and discuss scale-bridging strategies such as static and dynamic coarse-graining methods and multiresolution approaches. We close with a list of hard problems which still need to be solved in order to gain a comprehensive quantitative understanding of polymer systems.

KEYWORDS: *Multiscale phenomena, Polymer models, Multiscale modeling, Structural coarse-graining, Dynamic coarse-graining, Particle-continuum gap, Multiresolution*



I. INTRODUCTION

Multiscale problems are omnipresent in materials science. The properties of most materials result from a combination of many processes on vastly different length and time scales, ranging from electronic excitations and atomic or molecular vibrations on the Angstrom and femtosecond scale to material fatigue on time scales over several years. In polymeric systems, disentangling the different characteristic scales that determine their behavior is particularly difficult. This is because the relevant molecular length scales—which range from the scale of the local chemical monomer structure to the scale of chain conformations—strongly overlap with the relevant length scales of the next level of intermolecular and possibly supra-molecular organization, and these in turn overlap with the length scales of continuum mechanics on which materials are described in terms of elastohydrodynamic equations. Therefore, the all-inclusive, comprehensive modeling of a polymeric system¹ remains a formidable challenge despite decades of theoretical efforts.^{2–17}

In the present Perspective, we discuss some selected approaches to this problem, focusing on recent developments. Before doing so, we will quote a few examples of scale-bridging phenomena in polymers that inherently require multiscale descriptions.

The first and most basic example is the emerging viscoelasticity and viscoplasticity in *polymer rheology*, a field where the multiscale character of polymer-based systems is immediately apparent.¹⁸ Polymeric materials respond to applied stress with some time delay (memory), a clear signature of an

incomplete separation of time scales. This is because the time scales of intramolecular (internal chain) relaxation cannot be separated from the time scales of diffusion and intermolecular reorganization, in particular in the presence of entanglements.⁶

Another prominent classical multiscale phenomenon in polymer science is *polymer crystallization*,¹⁹ which involves local crystallization on the monomer scale, the formation of crystalline lamellae on the mesoscale, and the macroscale organization of lamellae, often into spherulites.²⁰ Already the local structure is not necessarily unique,²¹ but may result from a competition of several polymorphs depending on the processing.²² Predicting such polymorphs requires accurate theoretical descriptions at the electronic structure level²⁰ as well as multiscale modeling approaches to enable studying the kinetics of self-assembly.^{23,24} On the mesoscale, the mechanisms that determine and eventually constrain the growth of crystalline lamellae are still under debate.²⁵ One particular intriguing phenomenon is the “melt memory” effect:^{26,27} Even after melting a polymer crystal, the melt retains some knowledge about the previous structure and tends to recrystallize at previously crystalline positions after cooling. Recent systematic

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simulation studies by Luo, Sommer, and others have suggested that the thickness of crystalline lamellae is determined by the entanglement length in the melt prior to crystallization,^{28–33} consistent with the experimental observation that the time scale on which the melt memory survives roughly matches the time scale of re-entanglement kinetics.³⁴ Such findings illustrate how mesoscale structure (entanglements) can have a profound effect on local structure (local packing), and vice versa, in polymers. The associated time scales can be very large, which offers unusually versatile opportunities to control local structure by processing³⁵ (for example, in flow-induced crystallization^{36–40}) or by tiny chemical modifications.^{41,42} On the other hand, the mesoscale structure and dynamics determines the elastic and plastic response of the materials to deformations^{43,44} and the inhomogeneous stress fields in the materials, which in turn drive the large-scale structure formation and spherulite growth.⁴⁵

The interplay of multiple scales also determines the structural and dynamic properties of other *multiphase polymer materials*⁴⁶ that are highly heterogeneous and filled by internal interfaces, such as polymer blends,^{47,48} block copolymer melts and solutions,^{49–52} or foams.⁵³ It is particularly prominent in *polymer nanocomposites*,^{54–58} where fillers are introduced, e.g., to improve the mechanical properties of a polymeric matrix. The molecular origins of the resulting mechanical reinforcement are diverse, they include a redistribution of strain in the polymer matrix⁵⁹ as well as stretching of chains at the interfaces.⁶⁰ A detailed knowledge of the structure of the material on both local and mesoscopic scales is thus necessary to understand the macroscopic viscoelastic properties of the materials. Likewise, transport properties such as the thermal conductivity⁶¹ depend on the microscopic structure in the bulk matrix as well as at interfaces, i.e., the Kapitza resistance,^{62–64} and on the mesoscale shape and spatial distribution of the fillers.

Finally, *biomaterials* provide some of the most sophisticated polymer-based multiscale materials, due to their characteristic hierarchical structure. A prominent example is spider silk,^{65,66} which also showcases how the properties of such materials may crucially depend on the way how they have been processed (in this case spun).⁶⁷ Other examples are fibers made of collagen, which are abundant in mammals.^{68–71} Collagen is found in the extracellular matrix of tissues as different as skin, fascia, cartilage and bones, and is to a great extent responsible for their superior material properties. Twenty-nine types of collagen have been reported in the literature,⁶⁸ with the most frequent being collagen I, which is present in, e.g., dermis, tendon, and bone. The primary structure of collagen peptides is characterized by repeats of three residues Gly-X-Y, e.g., Gly-Pro-Hyp. The quaternary structure is a triple helix, where three polypeptide strands wrap around each other to form a helix of length ~300 nm, the tropocollagen. Staggered arrays of tropocollagen self-assemble (spontaneously⁷²) to fibrils, the building blocks of fibers (with size roughly 10 μm), which then aggregate to even larger structures.⁷³ Remarkably, the collagen triple helix seems to be only marginally stable; it melts at temperatures just slightly above, or even below the body temperature.⁷⁴ This suggests, on the one hand, that the triple helix is stabilized by the fibrillar/microfibrillar suprastructure,⁷² but also, on the other hand, that collagen frequently unfolds and refolds on a local scale. The combination of strength and softness would then contribute to the unique material properties of collagen tissues, to their elasticity, and to their capacity to dissipate sudden energy bursts.

In the context of *living tissues*, protein fibers are only one building block in the even more complex multiscale structures

of, e.g., bones^{75,76} or skin.⁷⁷ One important aspect of living materials is their dissipative character: They are kept alive by constant energy consumption and thus never reach thermal equilibrium, nor a thermally metastable state, but continuously produce entropy. Prominent representatives of such inherently nonequilibrium materials are protein filament structures which form the cytoskeleton of cells and are responsible for their mechanical elasticity as well as their motion and/or contraction.^{78,79} Another example is the recently discovered phenomenon of liquid–liquid phase separation (LLPS) in cells:^{80–87} Certain proteins mediate the formation of nanosized condensates in cells—so-called membraneless organelles—which helps to organize cellular content and possibly contributes to gene regulation. Whereas the phase separation itself is driven by thermodynamic interactions, the size and location of the droplets is most likely controlled by nonequilibrium, energy-consuming processes.

These selected examples illustrate the omnipresence of multiscale phenomena in polymeric systems, in seemingly simple ones such as one-component polymer melts as well as in complex ones such as functional polymers in a nonequilibrium living matter context. The multiscale character of polymers presents an outstanding challenge for modellers.

Synthetic polymer systems have been among the first materials for which systematic multiscale modeling methods have been developed, which related particle-based coarse-grained models to real polymers such as polyethylene,^{88–93} polycarbonates,^{94–98} and others.^{99,100} These early studies already addressed key challenges that are still subject of active research today: (i) The coarse-graining procedure, i.e. constructing coarse-grained models using input from quantum chemical calculations and/or atomistic models;^{88–91,94–96,99,100} (ii) reverse backmapping, i.e., the reconstruction of an atomistic configuration from a coarse-grained configuration;^{92,97,98} (iii) dynamic mapping,^{93,97} i.e., the question how to extract dynamical information from the coarse-grained simulations.

Since then, much progress has been made in the field of multiscale modeling of polymers and of soft matter systems in general, and several excellent reviews have highlighted different aspects of the problem, see, e.g., refs 4–8, 10, 12, 14–16, 101, and 102. Nevertheless, central challenges still persist. In the present Perspective, we discuss the current situation in the light of the state of the art and recent progress. We begin with a rough outline of models that are used to describe polymeric systems on different scales. Then we discuss a number of scale-bridging strategies that have been developed in the past and used for polymeric systems or might be applicable for them. We close with a brief outlook on open problems for the future.

II. SCALES IN POLYMERS

To set the stage, we begin with discussing the different scales that are involved in our multiscale picture of polymers and introduce classes of polymer models that are used to study polymer materials at these different levels.

II.A. Monomer/Oligomer Scale: The Scales of Chemical Specificity

The basic building blocks are the *monomers*. They can have a simple chemical structure, as in the case of many commodity polymers such as polystyrene, or a rather complicated structure, as in the case of biopolymers such as RNA, DNA, or proteins. The structure of the monomers on the monomer scale determines local properties such as the charges and the

polarization, the solubility in a solvent,¹⁰³ the existence and structure of a hydration shell,¹⁰⁴ the local affinity to surfaces,¹⁰⁵ or, in studies of polymer reactions, the monomer reactivity.¹⁰⁶ In general, these properties are also influenced by the larger-scale structure of polymer systems. For example, the effective monomer reactivity depends on the accessibility of the reactive sites, which is determined not only by the local electronic and steric monomer structure but also by the polymer conformation.^{106,107} Likewise, the effective charges and/or polarization of monomers depend on the local environment.^{108,109} In most cases, however, the corrections due to the larger-scale environment are small compared to the intrinsic value imposed by the monomer structure. To study polymers on the monomer scale, atomistic models are used, and in some cases quantum mechanical modeling is necessary.^{110,111}

The next level of organization is the *oligomer* scale, i.e., the scale of short polymer sections and monomer–monomer interactions. On that scale, cooperativity effects due to nonbonded or bonded interactions between monomers start to become prominent and even dominate. Here and in the following, the term “nonbonded” refers to general interactions between monomers of given types, no matter whether or not they belong to the same molecule (e.g., electrostatic interactions or van der Waals interactions), and the “bonded” interactions subsume the additional interactions between monomers that are close neighbors in the molecule (e.g., chemical bonds, bending or torsional potentials). Emerging properties of interest in the oligomer scale are, e.g., the effective monomer–monomer incompatibility,¹¹² ion-specific effects,^{113,114} the propensity to crystallize,¹⁹ or solvency/cosolvency and consolvency effects.^{114–120} Again, these properties also depend on the higher order organization, e.g., as has been discussed in the introduction for the case of crystallization. The modeling at this level is still often based on atomistic force fields, but chemically specific coarse-grained force fields such as the celebrated MARTINI model¹²¹ are starting to become useful; see also the recent review by Dhamankar and Webb.¹⁵ In such coarse-grained models, several atoms are lumped into one effective particle, and the (bonded and nonbonded) interactions between particles are determined either in a bottom-up fashion from atomistic simulations, in a top-down fashion from experimentally accessible data, or by a combination of the two. For an overview over coarse-graining approaches, we refer to the excellent review of Noid⁵ (see also below, section III.A.1).

II.B. Polymer Scale: The Scale of Conformations

The third level, the *polymer* scale, is the realm of classical polymer physics, where generic statistical mechanics approaches have celebrated successes.^{18,122,123} At this level, scaling laws have scored victories, both regarding static and dynamic properties of polymeric systems, and simple calculations based on “scaling blobs”^{123,124} can make meaningful predictions. This is because polymer molecules consisting of many identical monomer units start to exhibit universal behavior beyond a certain molecular weight. Therefore, renormalization groups concepts can be applied, according to which the fractal large-scale structure of polymer conformations does not depend on details of the local monomer structure. This results in the paradigm of the “Gaussian chain model”,¹⁸ which describes a polymer molecule as a random walk in space. In the case of complex heteropolymer molecules such as intrinsically disordered peptides (IDPs), applying scaling concepts is more challenging, but still at least partially successful.^{125–127} Theoretical models at this level are

mostly based on effective phenomenological parameters¹⁸ such as the Kuhn length, the famous Flory–Huggins χ -parameters characterizing polymer–solvent or monomer–monomer interactions, the monomer mobility, the effective monomer charge, and possibly the Debye screening length.

A number of generic coarse-grained simulation models have been proposed already decades ago to study polymer properties at this level: Lattice models, where polymers are represented by random self-avoiding walks on a lattice, and off-lattice models, where polymers are modeled as chains of interacting hard-core spheres connected by springs. Among the most prominent models of this type is the bond fluctuation model,¹²⁸ a lattice model where monomers occupy cubes on a lattice and can be connected by a finite set of bonds, and the Kremer–Grest model,¹²⁹ an off-lattice model that represents polymers as strings of hard-core spheres connected by nonlinear springs. Such models can be extended in various ways, e.g., to include bending potentials,^{130,131} attractive nonbonded interactions,¹³² or (in the case of polymer solutions) a hydrodynamic coupling to a fluid medium.¹³³ They have been used to verify scaling predictions^{131,134} and to study generic aspects of single polymer phase transitions such as chain adsorption or the coil–globule transition^{135–137} properties of polymer melts and blends¹³⁸ and even dynamical transitions such as the glass transition.^{139–141} To some extent, they can also be used to make quantitative predictions for chemically specific polymers. For example, recent work by Everaers and co-workers¹⁴² has shown that, for a wide range of commodity polymer melts, matching a single local property in melts of Kremer–Grest chains, the so-called dimensionless Kuhn number, is sufficient to reproduce the correct entanglement modulus.^{142,143} The Kuhn number is derived from microscopic quantities, i.e., the number of Kuhn segments in a volume of Kuhn length cube. The entanglement modulus is roughly proportional to a macroscopic quantity, the plateau shear modulus. Hence this example shows how simulations of a properly matched generic polymer model can be used to predict important characteristics of polymer materials. Milner has recently proposed a universal scaling theory of entanglements for melts and solutions of chains with arbitrary flexibility,¹⁴⁴ suggesting that similar approaches might also be successful for polymer solutions.

II.C. Interacting Polymers: The Blob Scale

The properties of *polymer systems* containing many polymers are often determined by conformational restructuring on scales that are much larger than the monomeric scale. On such scales, polymers behave in many respect like single soft, interpenetrating “blobs” or chains of such blobs. In polymer physics, the term blob often refers to a theoretical framework that allows for simple intuitive derivations of crossover phenomena between different scaling regimes in polymer solutions.^{123,124} Here we will use it more generally to describe the soft character of overlapping polymers.

In large-scale studies of interacting polymers, two novel classes of simulation models become increasingly popular that account for this soft character: Ultracoarse-grained particle-based models with soft potentials and density-based models. In soft potential models, coarse-grained units are assumed to represent lumps of a sufficiently large number of microscopic particles that they can interpenetrate each other. The nonbonded potentials are still described in terms of pair interactions between particles with positions \vec{r}_i and \vec{r}_j ,

$$U_{\text{nb}}[\vec{r}_k] = \sum_{i,j} V_{ij}(\vec{r}_i, \vec{r}_j) \quad (1)$$

possibly augmented by higher-order multibody potentials.¹⁴⁵ However, the potentials do not diverge at $\vec{r}_i = \vec{r}_j$. This is the case, for instance, for "dissipative particle dynamics" (DPD)-models^{145,146} or blob models.^{147–154}

In contrast, in density-based models,^{155–164} the nonbonded potentials are expressed as a functional of local number densities $\rho(\vec{r}) = \{\rho_\alpha(\vec{r})\}$ of coarse-grained monomer or solvent particles of type α , typically in the form of an integral over a "free energy density"

$$U_{\text{nb}}[\rho] = \int d^3r f(\vec{r}, \rho(\vec{r})) \quad (2)$$

where the function $f(\vec{r}, \rho(\vec{r}))$ depends implicitly on \vec{r} via $\rho(\vec{r})$ and may have an additional explicit \vec{r} -dependence (e.g., to account for external potentials and confinement effects). In the bulk, it is often taken to have a local quadratic form, defined in terms of Flory–Huggins-like interaction parameters

$$\frac{f(\rho(\vec{r}))}{k_B T} = \sum_{\alpha\beta} \chi_{\alpha\beta} \rho_\alpha(\vec{r}) \rho_\beta(\vec{r}) + \frac{\kappa}{2} \left(\sum_{\alpha} \rho_\alpha(\vec{r}) - \rho_0 \right)^2 \quad (3)$$

Here κ gives the compressibility of the polymer solution or melt, and we have assumed for simplicity that the volume fraction per bead of all entities is the same. We should mention that, in practical simulations, the value of κ is often reduced quite substantially compared to the real compressibility of polymers. This is done to avoid numerical instabilities and enable simulations with larger time steps.

To complete the definition of a density-based model, one must also specify how to determine the local densities ρ_α and how to formulate the corresponding spatially discretized version of the equations of motion. Often, the local densities are evaluated on a grid,¹⁵⁵ but other off-lattice variants based on weighted densities have also been proposed.^{161,165} When using a grid-based model in dynamical simulations, a second practical issue is how to determine the resulting forces on monomers—whether to directly take the derivative of the discretized Hamiltonian with respect to the monomer positions^{166,167} or whether to calculate a discretized force field and interpolate that.^{159,164,168} The former strategy guarantees that the simulation is grounded on a well-defined Hamiltonian, but it introduces lattice artifacts. The latter strategy gives more freedom to reduce the lattice artifacts and (approximately) restore momentum conservation in molecular dynamics simulations, but it does not guarantee that one samples a rigorously defined statistical ensemble in the limit of zero time step. Thus, the former approach is better suited for studying the statistical mechanics of the system, and the latter for studying processes where hydrodynamics is important.

Equation 3 defines one of the simplest density-based models, but numerous extensions are possible to make the model more flexible. One can add higher order terms,^{161,162} additional density fields that characterize, e.g., local orientation,^{169,170} charges,^{171,172} and/or nonlocal terms. For example, electrostatic interactions can be included in eq 2 by including the energy density of the electrostatic field generated by the charge density distribution $\rho(\vec{r}')$ and the corresponding interaction terms.¹⁷³

Both soft-potential models and models with density-based potentials are particle-based and describe the polymers as

connected chains of explicit monomers. They differ from hard-core models only in the type of nonbonded interactions. Removing the hard excluded-volume interactions, however, has a fundamental consequence: It removes topological interactions, i.e., the chains can now cross each other. This significantly changes the dynamic properties of the coarse-grained models and, in some cases, even the static structure.

Most prominently, the conformations of strictly two-dimensional polymers in dense melt are radically different for overlapping and nonoverlapping polymers.^{174–179} The configurations of overlapping polymers are rather open and the number of interchain contacts per monomer is roughly constant. In contrast, nonoverlapping polymers segregate from one another, and the number of contacts per monomer scales as $N^{-3/8}$ with increasing chain length N . This is because most open configurations are forbidden due to excluded-volume interactions. This effect is independent of dynamics and also persists in Monte Carlo simulations that simply sample the phase space.

In higher dimensions, the fraction of actually forbidden conformations in phase space is negligible, and the effect of hard excluded-volume interactions is more subtle. In polymer networks (gels, elastomers), and in systems of closed (ring) polymers, topological constraints partition the phase space, since a large set of energetically allowed conformations cannot be accessed kinetically from a given start configuration: For instance, initially concatenated rings cannot be separated and initially separated rings cannot be concatenated. As a result, ring polymers in a melt of nonconcatenated polymers are more compact than linear polymers, and their size (radius of gyration) scales differently as a function of N .¹⁸⁰ Capturing such effects with soft coarse-grained models is a formidable challenge. Narros et al.¹⁵³ have proposed a hierarchical multiblob approach, where the direct interactions between soft blobs (coarse-grained monomers) are supplemented by additional interactions between the centers of mass that account for the effect of topological interactions in a statistical sense. With this approach, they could reproduce the shrinking of ring polymers in melts with the correct exponent. However, other characteristics of large ring polymers in ring polymer melt, e.g., the dominance of double-folded conformations with primitive tree structure ("lattice animals"),^{181,182} are not captured. Interestingly, a recent comparison of simulation results using Kremer–Grest ring polymers with density functional calculations (which ignore topological constraints) has suggested that topological effects have no effect on the density profiles close to surfaces in sufficiently dense melts,¹⁸³ although they do seem to affect the thickness of depletion regions in semidilute solutions.

In contrast to ring polymer melts, melts of linear polymers are ergodic in phase space and blob models can mostly account for their static structure, at least on large scales. On small scales, there are deviations. For example, models with soft potentials tend to overestimate the frequency of small knots,^{184,185} in particular if the size of the excluded volume of monomers is comparable to that of the Kuhn segment.¹⁸⁴ More importantly, they fail to reproduce their dynamics at large N which is characterized by entanglements between polymers as already discussed earlier:^{9,18,186} According to the classic reptation picture, polymers undergo an effective one-dimensional diffusion in a tube, which is created by their entanglements with other polymers. Polymers interacting with soft potentials, however, do not reptate.¹⁸⁸ Schieber¹⁸⁹ and later Likhtman¹⁹⁰ have proposed an ingenious way to restore entanglements at the level of single-chain dynamics:^{9,191,192} They proposed to mimic

the effect of entanglements by virtual "slip links", discrete objects through which the chains must slip. This model has later been extended to multichain models where the slip links are fluctuating objects that connect different chains to each other.^{193–196} Such slip-link degrees of freedom introduce effective attractive interactions between polymers. However, the latter can be calculated analytically and subtracted from the basic potential function, e.g., eqs 1 or 2, to eliminate their effect on the static behavior.^{193,194} Wu et al. and Behbahani et al. have recently demonstrated the potential of multichain slip-link approaches in ultracoarse-grained simulations of real commodity polymers such as polyethylene,¹⁹⁷ polystyrene,¹⁹⁸ and polybutadiene¹⁸⁷ (see Figure 1). Introducing slip links can also help to restore the correct elastic and rheological properties in soft-potential based models for elastomers.¹⁹⁹

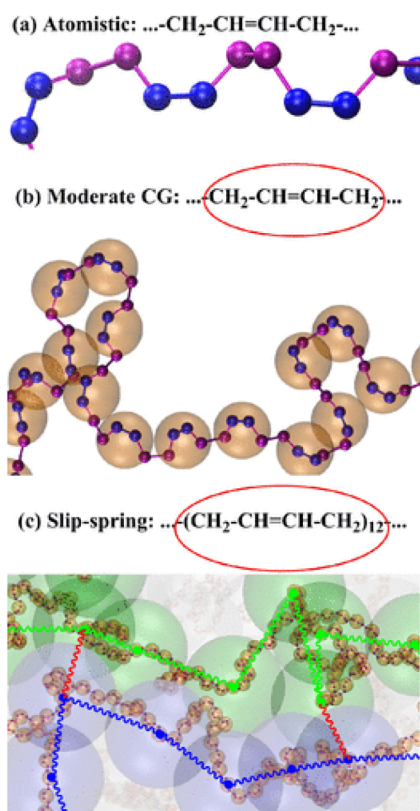


Figure 1. Different levels of description of *cis*-1,4-polybutadiene (cPB) in ref 187. (a) United atom model. (b) Structurally coarse-grained model with hard core interactions. (c) Soft potential model with slip-links. The dynamical single-chain and viscoelastic properties can be mapped onto each other and are also in good agreement with experimental data. Reproduced from ref 187. Copyright 2021 American Chemical Society.

II.D. Mesoscopic Scale: Transition to Field Theories

The next level is the scale of *mesoscale organization*, i.e., structure formation in inhomogeneous polymer systems. Emerging phenomena at this scale are the nucleation of crystallites in semicrystalline polymers,¹⁹ phase separation and demixing,⁴⁶ wetting phenomena, or self-assembly.⁵¹

Apart from the coarse-grained particle-based polymer models with hard or soft interactions discussed in sections II.B and II.C, a new tool for investigating polymer systems on such scales are *field-theoretic approaches*.^{201–203} The most common starting

points for the derivation of such approaches are density-based models such as the one defined by eq 2. By field theoretic manipulations such as delta functional transformations^{204–206} or Hubbard-Stratonovich transformations,^{201,207,208} one can rewrite the partition function of this system as an integral over fluctuating real and imaginary fields. For example, the delta functional transformation of the model (eq 2) yields the following expression for the partition function:²⁰⁵

$$\mathcal{Z} \propto \int_{i\infty} \mathcal{D}\underline{W} \int_{\infty} \mathcal{D}\underline{\rho} \exp(-\mathcal{F}/k_{\text{B}}T) \quad (4)$$

with

$$\frac{\mathcal{F}[\underline{\rho}, \underline{W}]}{k_{\text{B}}T} = \int d^3r f(\vec{r}, \underline{\rho}(\vec{r}))/k_{\text{B}}T - \sum_{\alpha} \int d^3r \rho_{\alpha}(\vec{r}) W_{\alpha}(\vec{r}) - \sum_j n_j \ln(Q_j/n_j) \quad (5)$$

(in the canonical ensemble) where $\underline{W}(\vec{r}) = \{W_{\alpha}(\vec{r})\}$ denotes a vector of fluctuating imaginary auxiliary fields $W_{\alpha}(\vec{r})$, j sums over different polymer types, and $Q_j[\underline{W}]$ is the single-chain partition functions of polymers of type j without nonbonded interactions in the fluctuating external field $\underline{W}(\vec{r})$.

Taking these expressions as a starting point, one can make several approximations: First, one can replace the integral (eq 4) by a saddle point approximation, which amounts to approximating the free energy of the system by the extremum of \mathcal{F} in eq 5. Remarkably, the extremum for \underline{W} is not located on the original imaginary integration domain, but is purely real. The approximation results in the so-called *self-consistent field* (SCF) theory,^{205,206,209} one of the most powerful mean-field approximation for inhomogeneous polymer systems, which can often predict real interfacial structures in polymers at an almost quantitative level.²⁰⁶ Figuratively speaking, the SCF theory describes polymer systems as assemblies of independent chains, each in the ensemble-averaged field of the surrounding chains. The averaging approximation is good if chains interact with many other chains, which is true for chains of high molecular weight since they overlap with each other. In three-dimensional melts of linear polymers, the degree of interchain interactions can be characterized by the so-called invariant polymerization index $\bar{N} = b^6 \rho_0^2 N$, where b is the statistical segment length, and N is the number of segments in a polymer chain. For $\bar{N} \rightarrow \infty$, the SCF approximation becomes exact. Experimentally relevant values of \bar{N} are of order 10^2 – 10^4 .

A second approximation to eq 4 consists of applying a partial saddle point approximation with respect to the auxiliary fields $W_{\alpha}(\vec{r})$ only. Thus, the functional $\mathcal{F}[\underline{\rho}, \underline{W}]$ is extremized with respect to \underline{W} , giving self-consistent equations for $\underline{W}[\underline{\rho}]$, which have, again, a real solution $\underline{W}(\vec{r})$. This procedure turns \mathcal{F} into a real-valued density functional $\mathcal{F}[\underline{\rho}]$. It serves as starting point for dynamic mean field theories of polymers which have the structure of continuum theories but retain some knowledge of the macromolecular architecture of polymers. The simplest Ansatz of this kind is the purely diffusive equation of motion^{210–221}

$$\partial_t \underline{\rho}(\vec{r}, t) = \nabla_r \int d^3r' \underline{\Delta}(\vec{r}, \vec{r}') \nabla_{r'} \underline{\mu}(\vec{r}', t) \quad (6)$$

with $\underline{\mu}_{\alpha}(\vec{r}, t) = \delta \mathcal{F} / \delta \rho_{\alpha}(\vec{r}, t)$. In the context of the Hohenberg–Halperin classification²²² of dynamic critical phenomena (see section II.E), eq 6 corresponds to so-called "model B"

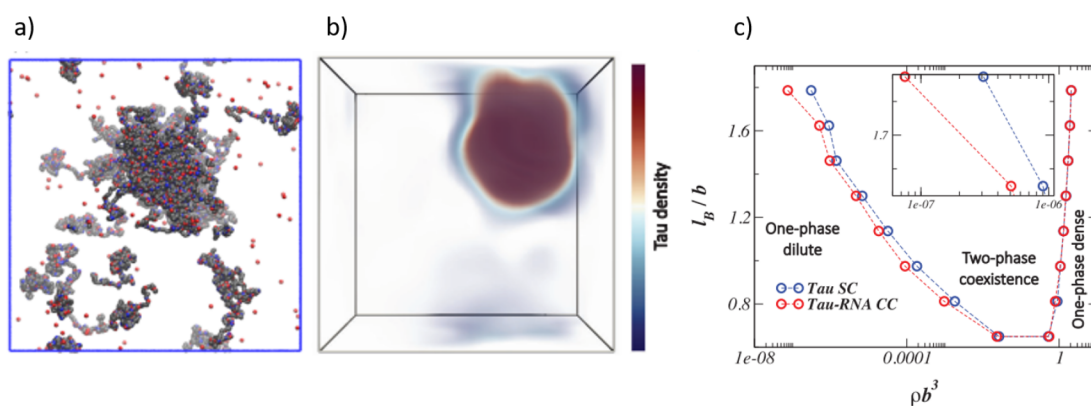


Figure 2. Coarse-grained simulations of liquid–liquid phase separated droplets of tau proteins.²⁰⁰ (a) Particle-based CG model using a Kremer–Grest type representation of chains. (b) FTS model, studied by Complex Langevin simulations. (c) Phase diagram obtained from FTS simulations as a function of Bjerrum length l_B and tau-density ρ rescaled with the statistical segment length b (blue curve). The red curve shows the corresponding phase diagram for mixtures of Tau and RNA. Adapted with permission from ref 200. Copyright 2021 John Wiley and Sons.

dynamics. The mobility matrix function $\Delta(\vec{r}, \vec{r}') = \{\Lambda_{\alpha\beta}(\vec{r}, \vec{r}')\}$ describes the motion of monomers at position \vec{r} in response to a local thermodynamic force $(-\nabla_{\vec{r}} \mu(\vec{r}, t))$ and may be nonlocal to account for the effect of chain connectivity. Possible extensions include the coupling to equations of fluid dynamics in order to account for hydrodynamics,^{223–226} the inclusion of additional order parameters to account for local chain ordering,²²⁷ or the introduction of a time-delayed response functions to account for memory.^{228,229}

Going beyond the mean-field approximation, *field-theoretic simulations* (FTS), aim at sampling the full partition function (eq 4). The field of FTS is relatively new and, so far, restricted to static simulations. An important problem that needs to be overcome is dealing with the imaginary integration domain of \underline{W} in the integral (eq 4). Since the $W_\alpha(\vec{r})$ are imaginary, the “action” \mathcal{F} in eq 5 is a complex, rapidly oscillating quantity, which leads to a sign problem. Pioneered by Ganesan and Fredrickson,²³⁰ one approach to overcoming this problem is to use the so-called “Complex Langevin” simulation method, which involves solving Langevin equations in the entire complex plane, in the case of eq 4 for both the \underline{W} and ρ degrees of freedom.

If the underlying nonbonded potential functional is a quadratic functional of the densities $\underline{\rho}(\vec{r})$ as, e.g., in eq 5, one can reduce the number of fluctuating fields by a factor of 2 by applying a Hubbard–Stratonovich transformation instead of a delta functional transformation, which significantly reduces the computational costs. Complex Langevin simulations based on this approach have been used by Fredrickson and co-workers and other groups to study, among other, fluctuation effects in diblock copolymer phase diagrams,^{202,230} polymer nanocomposites,²³¹ polyelectrolyte complexation,²⁰² and liquid–liquid phase separation of intrinsically disordered proteins.^{200,232} Figure 2 shows a FTS simulation droplets formed from tau proteins, strong polyampholytes which undergo liquid–liquid phase separation due to self-coacervation.

In dense melts of polymers containing only two types of monomers A and B, a second approach becomes possible,^{203,217,218,233–238} which has been applied with considerable success by Matsen and co-workers to study block copolymer systems.²³⁵ In that case, the Hubbard–Stratonovich transformation results in a functional integral over two fluctuating fields, an imaginary one which can be associated with density fluctuations and a real one which describes the composition fluctuations. In nearly incompressible melts, the density

fluctuations have little influence on the composition fluctuations that determine the phase behavior. Therefore, one may apply a partial saddle point approximation regarding the density fluctuations only, and obtains a purely real fluctuating field theory, which can be treated, e.g., by standard Monte Carlo methods.^{236,239} Comparisons with Complex Langevin simulations^{236,239} have shown that the partial saddle point approximation is indeed accurate in dense melts. The advantage of the approach is that it allows more easily to access highly incompressible melts at experimentally relevant polymerization indices.²⁰³

In many cases, fluctuation corrections mainly shift phase transition temperatures or change the order of a transition from second order to weakly first order, but there are situations where they may fundamentally change the properties of a system. One prominent example is the “microemulsion channel” in balanced mixtures of A,B homopolymers and A:B diblock copolymers. Upon increasing χN , SCF calculations predict a demixing transition at low copolymer content, and an ordering transition to a periodic lamellar phase at high copolymer content. According to the SCF theory, both transitions meet at a so-called “Lifshitz critical point”, where the lamellar thickness of the periodic phase diverges. In reality, generic theoretical considerations²⁴⁰ suggest that the Lifshitz critical point has a lower critical dimension of four, meaning that fluctuations will invariably destroy it in three (or fewer) dimensions. The fate of the Lifshitz point in lower dimensions has long remained unclear, but was recently revealed by field-theoretic simulations of Vorseelaers, Spencer, and Matsen:^{233,234} It splits up into a critical end point and a tricritical point (see Figure 3). This example also demonstrates how simulations of polymer systems can give insights onto fundamental questions in statistical mechanics.

II.E. Macroscopic Scale: The Engineering Scale

Finally, at the *macroscopic* level, the focus lies on properties of polymeric materials that are of direct interest for engineers: Mechanical stability, microstructure, stress distribution, viscoelasticity, constitutive relations, and aging phenomena. Emerging phenomena that are studied on such scales are, for instance, polymeric flow patterns in complex geometries²⁴² but also inherently inhomogeneous processes such as viscoelastic phase separation,²⁴³ foaming,^{244,245} or crack formation.²⁴⁶ On macroscopic scales, materials are described by a set of characteristic

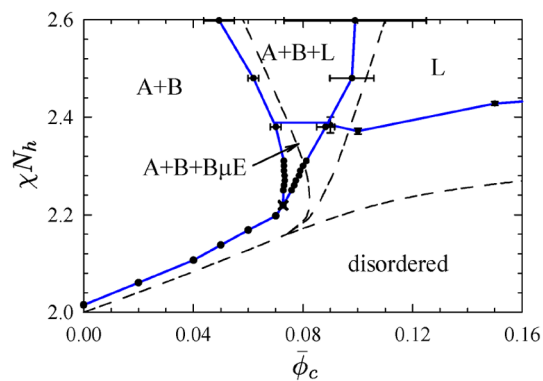


Figure 3. Fluctuation effects on the Lifshitz point in the phase diagram of ternary A/B/AB homopolymer/diblock melts, as revealed by field-theoretic simulations in refs 233 and 234. Dashed line shows mean-field result, symbols connected by solid lines show the simulation results. Reprinted with permission under a Creative Commons CC BY 4.0 License from ref 235. Copyright 2021, Matsen/Beardsley.

continuous fields and corresponding transport equations. They are typically constructed somewhat heuristically based on general symmetry considerations and conservation laws, following the spirit of the famous Hohenberg–Halperin classification of dynamic critical phenomena.²²² For example, so-called “model A” dynamics is used to describe relaxation processes where conservation laws are not important, “model B” dynamics is used to describe diffusive processes where only the local conservation of one “order parameter” (e.g., the polymer volume fraction) matters (an example is eq 6), “model C” dynamics describes processes where other conserved mass densities also become important, and “model H” additionally accounts for local momentum conservation and convection in order to describe stress, flow, and hydrodynamic phenomena.

It should be noted that continuum models are much less transferable than lower level models. Above the glass transition, cross-linked polymer networks are best described by elasticity theories, using displacement fields as primary field variables (e.g., refs 247, 248), and constitutive equations that establish a relation between the stress tensor and the strain tensor. In contrast, fluids of un-cross-linked polymers are described by hydrodynamic models in terms of flow fields, and constitutive equations relate the stress tensor with the strain rate tensor. Below the glass transition, polymer materials behave like solids, but plastic flow is also possible in response to high stresses. This can be addressed by distinguishing between reversible elastic deformations and irreversible plastic deformations.^{249–252} Even within the realm of continuum models, multiscale techniques are still necessary to bridge between micromechanical models as discussed here and mechanical models that describe objects made of polymers on truly macroscopic scales.^{253,254}

In the following, we will focus on models for polymeric fluids. These often combine a hydrodynamic description with a simplified microscopic model for viscoelasticity, in order to account both for flow and internal relaxation processes. An important tool in the construction of such models is the so-called *convected derivative*, a concept originally introduced by Oldroyd.²⁵⁵ It describes convection with respect to a “material frame” of comoving material particles and thus in some sense generalizes the substantial derivatives in fluid dynamics to tensorial quantities. To explain the convected derivative, we first recapitulate the idea of the substantial derivative, which is a standard concept in fluid mechanics: Consider a fluid flow

characterized by a flow field $\vec{u}(\vec{r}, t)$ carrying a scalar field $\Phi(\vec{r}, t)$. Let $\Phi^{(L)}(\vec{r}, t)$ be the corresponding scalar field in the comoving (Lagrangian) frame with $\Phi(\vec{r}, 0) = \Phi^{(L)}(\vec{r}, 0)$. The substantial derivative is defined such that it describes the evolution of the scalar field $\Phi(\vec{r}, t) = \Phi^{(L)}(\vec{r} - \vec{u}t, t)$ in the comoving frame, i.e.,

$$\frac{d}{dt}\Phi := \partial_t\Phi^{(L)} = \partial_t\Phi + (\vec{u} \cdot \nabla)\Phi \quad (7)$$

When generalizing this concept to tensorial fields $\mathbf{Q}(\vec{r}, t)$ (or $Q_{ij}(\vec{r}, t)$ in coordinate notation), following Oldroyd, one must take into account the deformations of the coordinates of \mathbf{Q} in the comoving frame. They are determined by the deformation rate field $\mathbf{G} = \nabla\vec{u}$ (or $G_{ij} = \partial_j u_i$ in coordinate notation). As before, we choose $\mathbf{Q}(\vec{r}, 0) = \mathbf{Q}^{(L)}(\vec{r}, 0)$. For contravariant tensors \mathbf{Q} , the relation between \mathbf{Q} and $\mathbf{Q}^{(L)}$ in the limit $t \rightarrow 0$ is then given by $\mathbf{Q}(\vec{r}, t) = (\mathbf{1} + \mathbf{G}^T t)\mathbf{Q}^{(L)}(\vec{r} - \vec{u}t, t)(\mathbf{1} + \mathbf{G}t)$. This motivates the definition of the upper convected derivative

$$\overset{\circ}{\mathbf{Q}} := \partial_t\mathbf{Q}^{(L)} = \partial_t\mathbf{Q} + (\vec{u} \cdot \nabla)\mathbf{Q} - \mathbf{G}^T\mathbf{Q} - \mathbf{Q}\mathbf{G} \quad (8)$$

The corresponding consideration for covariant tensors yields the lower convected derivative

$$\overset{\hat{}}{\mathbf{Q}} := \partial_t\mathbf{Q} + (\vec{u} \cdot \nabla)\mathbf{Q} + \mathbf{G}^T\mathbf{Q} + \mathbf{Q}\mathbf{G} \quad (9)$$

The concept of convective derivatives provides a framework for deriving constitutive relations in viscoelastic materials in a geometrically consistent manner. For example, the so-called upper convected Maxwell model

$$\boldsymbol{\sigma} + \lambda \overset{\circ}{\boldsymbol{\sigma}} = 2\eta\mathbf{D} \quad (10)$$

with $\mathbf{D} = (1/2)(\mathbf{G} + \mathbf{G}^T)$ describes a material with a linear steady-state stress–strain relation $\boldsymbol{\sigma}_{\text{steady}} = 2\eta\mathbf{D}$, where the stress tensor, $\boldsymbol{\sigma}$, relaxes in a simple exponential manner toward its steady-state value with relaxation time λ .

More sophisticated viscoelastic models are typically based on one of two approaches:¹⁰ Either they use phenomenological considerations to construct more complicated expressions for the relaxation of the stress tensor and/or its steady-state value, or they select a simplified molecular model for the polymers and use kinetic theory to derive approximate expressions for the stress tensor. One popular starting point of the second kind is to consider a Newtonian fluid filled with noninteracting elastic dumbbells, i.e., two beads connected by “Finitely Extensible Nonlinear Elastic” (FENE) springs, with a spring constant $k(R)$ that diverges if the distance R of the beads exceeds a limiting value. A Fokker–Planck equation for the conformation of the dumbbells is then coupled to the Navier–Stokes equations via two convective contributions to the Fokker–Planck equation (one for the center of mass and one for the relative distance of beads) and an extra stress term in the Navier–Stokes equations. Many macroscopic models for polymer fluids can be seen as approximations to this FENE model. The most prominent one is the Oldroyd-B model, one of the first models for polymer fluids,²⁵⁵ which replaces the FENE spring by a regular linear Hookean spring.²⁵⁶ This simplifies the mathematical analysis, however, it leads to unphysical singularities under certain flow conditions where the dumbbells stretch to infinity. Another approximation is the Peterlin model (FENE-P), where the nonlinear spring constant $k(R)$ is replaced by an averaged value $k(\langle R \rangle)$.^{257,258}

In order to avoid mistakes when constructing such models, considerable care has to be taken to ensure that they are thermodynamically consistent.^{259,260} Several mathematical

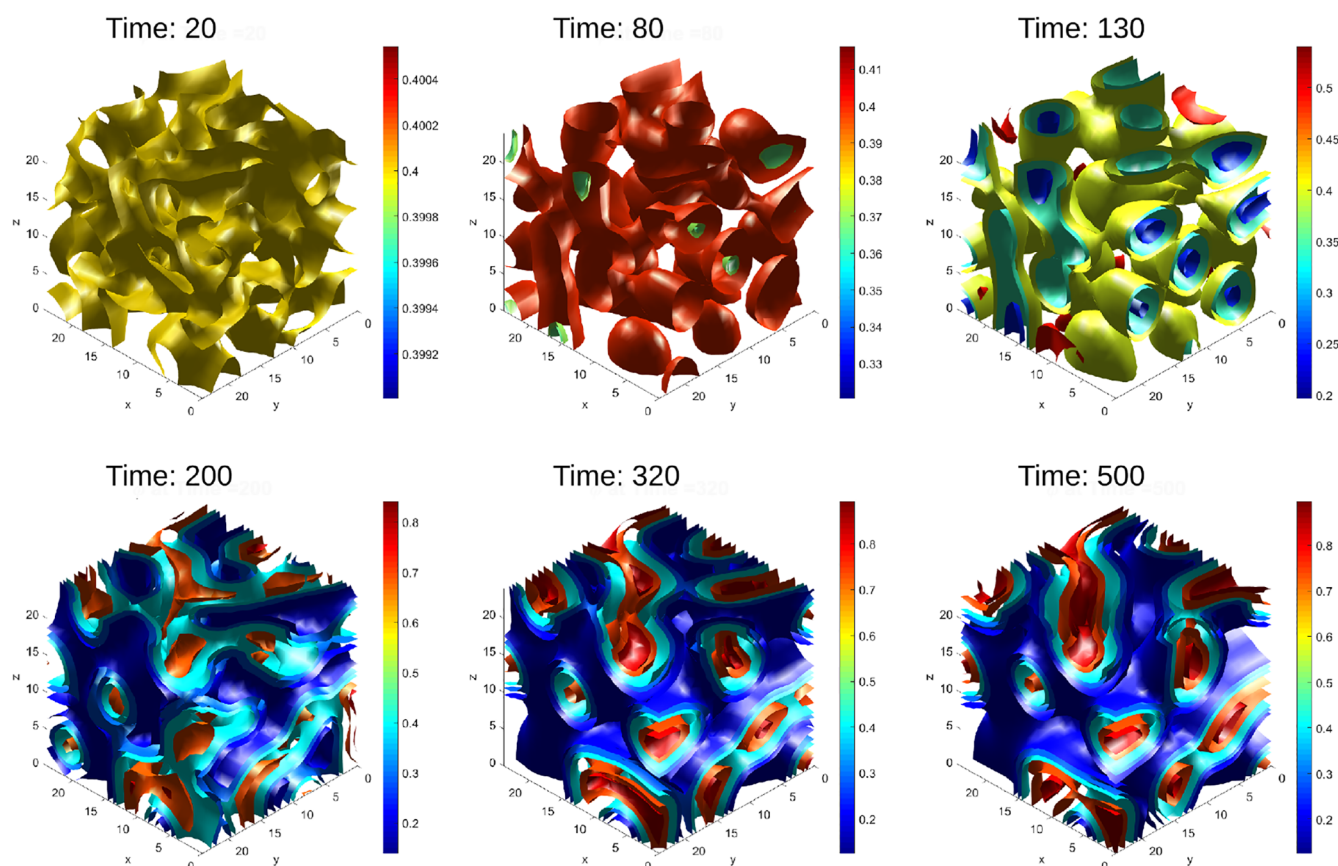


Figure 4. Spinodal phase separation in a continuous viscoelastic model (similar to Figure 1 in ref 241). The numerical simulation is based on a Lagrange–Galerkin finite element method. Courtesy of M. Lukáčová-Medvid'ová.

frameworks have been developed which help to enforce consistency, the most rigorous being the GENERIC framework that makes a strict distinction between antisymmetric reversible and symmetric irreversible (dissipative) contributions to the dynamical equations.²⁶¹ It should be noted that not all published macroscopic models are thermodynamically consistent. Schieber and Cordoba have recently developed a simplified set of requirements that allows one to perform basic consistency tests without having to apply the full GENERIC machinery.²⁶⁰ Another, even more difficult, question is to prove that the models actually have solutions for arbitrary initial conditions. Global existence results for weak solutions of the Peterlin model have recently been obtained by Masmoudi²⁵⁶ and, regarding a class of generalized Peterlin models, by Lukáčová-Medvid'ová et al.^{262,265}

The study of inhomogeneous polymer *solutions* is particular challenging due to the vastly different mobilities of polymer and solvent molecules. Quite generally, large dynamical asymmetries between components of a demixing system often result in unconventional network-like pattern formation and novel dynamic scaling exponents²⁶⁴ compared to standard model B or model H demixing, because the domains of the slow phase tend to behave like viscoelastic objects. This phenomenon was first discovered by Tanaka in 1993²⁶⁵ who termed it “viscoelastic phase separation”, and it is still a subject of active research.^{243,266–271} Theoretical models typically build on the two-fluid model proposed by Doi and Onuki²⁷² and Milner,²⁷³ which include a coupling between elastic stress and concentration. Based on this idea, Zhou et al. proposed a number of

phenomenological models for viscoelastic phase separation, paying particular attention to thermodynamic consistency.²⁶⁹ Spiller et al.²⁷⁰ have recently taken the kinetic approach and derived a two-fluid model for solutions of Hookian dumbbells which is consistent with the GENERIC formalism. Brunk and co-workers have analyzed a number of models for viscoelastic phase separation from a mathematical point of view and proved the existence of weak solutions.^{241,271,274} An example of a numerical simulation of one of their models is shown in Figure 4.

III. SCALE-BRIDGING STRATEGIES

In the previous section, we have discussed the hierarchy of models that have been designed and used to study polymeric systems on different scales. In many cases, however, using a single model is not sufficient to fully characterize a material of interest. Thus, multiscale modeling techniques must be applied, which combine different scales in one simulation, or at least establish quantitative connections between different scales. The key to multiscale modeling is coarse-graining, i.e., the art of designing high-level models with few degrees of freedom (“coarse-grained (CG) models”) that capture the essential features of an underlying “fine-grained (FG)” system.

Classical coarse-graining strategies traditionally follow one of two philosophies:⁵ “Top-down” CG models are designed based on physical intuition without direct input from FG simulations. Examples are generic top-down models such as the bond fluctuation model¹²⁸ and the Kremer–Grest model¹²⁹ discussed in section II.B, which are used to study generic properties of polymer systems, but also chemically specific top-down models

such as the MARTINI model,¹²¹ which use experimental information such as solubility parameters to match interaction parameters. In contrast, “bottom-up” CG models are constructed from FG simulations in a systematic manner such that they capture certain structural or thermodynamic properties of interest. This is strategy is commonly adopted to derive classical atomistic force fields from electronic structure calculations, and it is also used to construct higher-level models. In addition to bottom-up and top-down approaches, hybrid approaches are becoming increasingly popular that integrate information from different sources—FG simulations as well as experiments^{275–278} and data-driven methods that apply machine-learning methods.^{15,102,278}

Numerous coarse-graining and scale-bridging strategies have been proposed over the past decades (see refs 4–8, 10, 12, and 14–16 for review articles), and giving a comprehensive overview is beyond the scope of the present Perspective. Instead we will give a very personal view on different aspects of the coarse-graining problem with a focus on bottom-up coarse-graining, on lessons learned from the past, and challenges for the future.

Formally, defining the coarse-graining task seems quite obvious: Given a microscopic dynamical system with N degrees of freedom and corresponding equations of motion, define a reduced set of n representative collective variables and derive their dynamical equations from those of the microscopic system. This idea is old, and projection operator techniques to derive coarse-grained equations have been proposed already in the 1960s by Zwanzig and Mori.^{279–281} They were used, among others, to derive equations of fluctuating hydrodynamics for simple and complex fluids.^{282,283} In recent years, the Mori–Zwanzig formalism has attracted increasing interest in the coarse-graining community, mostly thanks to the work of Español and co-workers who promoted it as a practical tool to construct, e.g., dynamic density functional theories²⁸⁴ or particle-based DPD models.²⁸⁵ In principle, projection operators allow one to derive *exact* dynamical equations for the chosen coarse-grained variables. However, these are complex integro-differential equations that cannot be reduced to practically useful model equations, e.g. stochastic equations, without substantial further approximations. Even more seriously, Glatzel and Schilling have recently argued that the dynamic equations for the coarse-grained variables $A_i(t)$ cannot necessarily be related to a potential of mean force^{17,286} $U[A_i]$. Their claim is consistent with a discussion by Zwanzig in ref 287, who pointed out that the memory kernel in the linear Mori–Zwanzig equations absorbs some of the nonlinearities of a nonlinear conservative potential in the FG equations. Unfortunately, this implies that the resulting CG models are not necessarily compatible with the GENERIC framework²⁶¹ and its clear distinction between external driving forces, conservative interactions, and dissipative forces. As discussed earlier, the GENERIC structure helps to enforce thermodynamic consistency and ensure, by construction, that violations of the second law of thermodynamics are not possible in a CG model. Giving up this structure thus represents a serious drawback. Luckily, recent work by Vroyland and Monmarché suggests a possible way out of this dilemma. Using the Mori–Zwanzig formalism and considering a single CG particle, they showed that it is possible to derive a GLE that complies with the GENERIC structure, if one allows for position dependent memory kernels.²⁸⁸

One may be tempted to set aside these problems and design CG models that primarily target static equilibrium properties.

One can then use the partition function of the microscopic system as the starting point and integrate out the N microscopic degrees of freedom while constraining the n CG variables, which directly gives a “potential of mean force” or “free energy landscape” $U[A_i]$. In general, however, simple analytic expressions for $U[A_i]$ are not available, such that a simulation of the exact CG model is as expensive, from a computational point of view, as the simulation of the FG model. Thus, further approximations must again be made such as, e.g., rewriting $U[A_i]$ as a sum of effective pair or low order multibody potentials.

Finally, already the identification of meaningful coarse-grained variables represents a challenge in itself—in particular if the coarse-grained model is expected to capture several very different aspects of the underlying FG model. This leads to the well-known problem of *representability*: A CG model that reproduces the structure of the FG model does not necessarily have the correct thermal properties and vice versa. Moreover, a CG model that was constructed for one state point (e.g., one density), not necessarily captures the properties of the FG model at another state point (another density). The latter so-called *transferability* issue will obviously cause problems when using CG models for studying strongly inhomogeneous systems.

In sum, coarse-graining is bound to be a somewhat “dirty” business. This is a direct consequence of the famous “no free lunch” theorem: Unfortunately, it is not possible to simplify a complex problem just by rewriting it in terms of fewer variables. Coarse-graining is effectively an optimization problem which requires many compromises and a high level of physical and chemical intuition. The coarse-graining philosophy rests on the assumption that the large-scale structure of materials can be understood without explicit knowledge of microscopic details. In the case of polymers, one hopes that this assumption is justified due to their repetitive molecular structure, the high level of conformational disorder, and the dominant role of entropy.

We will now discuss selected aspects of coarse-graining in polymeric systems or, more generally, soft matter systems.

III.A. Static Coarse-Graining

III.A.1. Structure-Based Coarse-Graining. Structure-based coarse-graining techniques are typically used to design particle-based CG models with the goal to reproduce structural properties of the FG system such as spatial correlation functions. The CG variables are the positions \mathbf{R}_i of CG particles, and the optimization task consists in finding the best approximation for the free energy landscape $U[\mathbf{R}_i]$ or the configuration dependent force field $\mathbf{F}_i[\mathbf{R}_i]$ in the phase space of the CG variables. Regarding equilibrium static coarse-graining, the field is already quite advanced. The CG bonded interactions can be calculated in a straightforward manner by sampling, e.g., bond length and bond angle distributions in small reference simulations. To determine nonbonded CG interactions, researchers can use the open-source package VOTCA²⁸⁹ (www.votca.org) and select between a range of established methods^{5,7} such as inverse Monte Carlo (IMC),²⁹⁰ iterative Boltzmann inversion (IBI),^{291–295} force matching (FM),^{296–300} or relative entropy (RE) minimization between the CG and the FG distribution.³⁰¹ Alternatively, they can employ the framework of the generalized Yvon–Born–Green (g-YBG),^{302–304} or use artificial neural networks.^{102,305,306} Noid and co-workers have pointed out that the quality of nonbonded CG force fields can be greatly improved if one distinguishes between CG monomers that have different local connectivities within a molecule,^{307,308} e.g., between middle and end segments.

One paradigmatic problem in structural coarse-graining is to construct pair potentials from radial distribution functions (RDFs) of particles as determined, e.g., from FG simulations. This is known as the inverse Henderson problem. As proved in 1974 by Henderson for finite systems with fixed particle number³¹⁰ and very recently by Frommer et al.^{311,312} for the thermodynamic limit, the problem has a unique solution for a rich class of interaction potentials which includes, among other the so-called Lennard-Jones type potentials.³¹³ Nevertheless, the problem is ill-posed in the sense that a small noise in the RDF can lead to large changes in the potentials. In other words, quite dissimilar potentials can produce almost identical RDFs^{309,314} (see also Figure 5). This opens possibilities to optimize pair potentials not only with respect to structural properties, but also to other properties as well. Building on this idea, Hanke and co-workers have recently developed novel integral equation-based methods that allow one to solve the inverse Henderson problem with additional constraints,^{315,316} such that the resulting CG model reproduces both the structural correlations and the

thermodynamic properties of the microscopic system.³¹⁶ When applying such methods, one should keep in mind that the RDFs obtained from FG simulations may suffer from finite-size effects. Cortes-Huerta and co-workers have recently investigated this in the context of Kirkwood–Buff integrals^{317,318} and proposed expressions for finite-size corrections in liquid solutions.³¹⁷ In the presence of elastic interactions, finite size effects persist even in large systems and extrapolation procedures must be applied.^{319,320}

An interesting alternative way of dealing with the representability problem has been proposed by Lebold and Noid.^{321,322} Rather than trying to find one CG model that captures both the energetics and the structure of the FG model, they suggest to explicitly keep track of energetic and entropic contributions to the potential of mean force^{321,322} in the CG simulation. Thus, the effective potential is split up as

$$U[\mathbf{R}_i] = U_W[\mathbf{R}_i] - TS_W[\mathbf{R}_i] \quad (11)$$

where U_W is constructed such that it gives, on average, the energy of the *fine-grained* system with collective variables constrained to \mathbf{R}_i . The potential U is obtained by standard structural coarse-graining methods, and the potential U_W is determined using a minimization method similar to least-squares fitting. When analyzing CG simulation trajectories, the potential U_W can then be used to calculate observables that depend on energy. As a side effect, this approach also allows one to estimate the expected change in the potential of mean force at a different temperature with remarkable accuracy.³²² Among others, it could be used to overcome sampling problems in the microscopic reference system, e.g., close to a glass transition.³²³

Going beyond pure pair potentials, higher-order multibody potentials^{324–328} or density-dependent potentials^{329–338} offer additional flexibility which can be exploited to develop CG models with improved transferability properties.³³⁹ In particular, density-dependent potentials provide a comparatively straightforward way of accounting for the local environment of interacting CG particles that may undergo liquid–vapor phase separation,³⁴⁰ and they are quite popular in empirical models with soft potentials such as (many-body) DPD¹⁴⁵ or models with density-based interactions.¹⁶⁵ Such empirical soft potential models are often set up as a sum of two contributions: Local density-dependent repulsive interactions between particles that account for the effect of excluded volume interactions, and density-independent attractive interactions that account for cohesion. The functional form of the two terms is usually postulated, but they can also be derived in a bottom-up fashion from FG simulations, e.g., by a combination of force matching and relative entropy minimization.^{336,338} Since one has some freedom how to distribute the forces between different contributions, the results are not unique;³³⁶ they depend on the coarse-graining procedure. This gives freedom which can be exploited to further optimize the potentials with respect to representability and transferability.

We should note that density-dependent potentials also have interesting applications beyond liquid–vapor systems, e.g., in ultracoarse-grained descriptions of compressible fluids or in coarse-grained descriptions of responsive materials where the shape of CG particles depends on their local environment.³⁴¹

In other situations where local orientations of molecules or monomers are important, it might be desirable to include multibody potentials³⁴² that also depend on the local conformation, such as three-body Stillinger–Weber type potentials that depend on the local angles between the

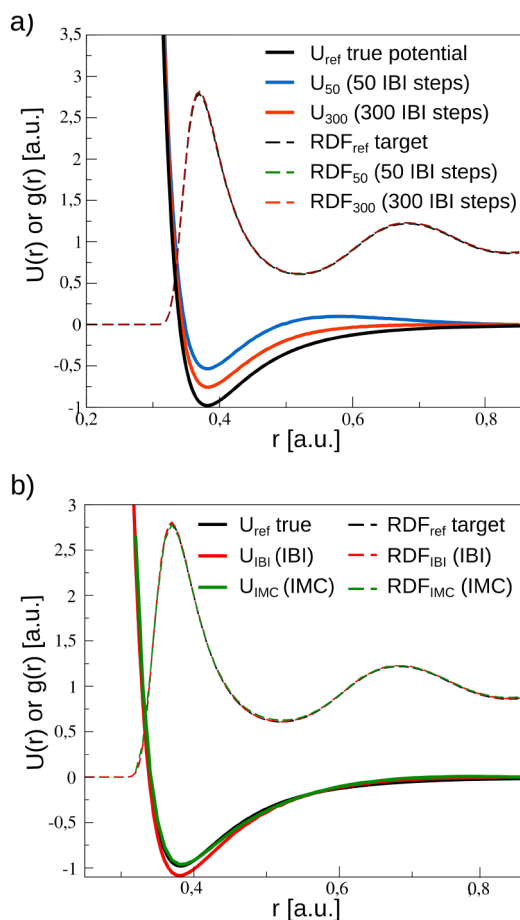


Figure 5. Uncertainties in the reconstruction of pair potentials from pair correlation function, see also.³⁰⁹ In this example, the target RDF is taken from simulations of a binary Lennard–Jones mixture; hence, the true potential (black solid line) is well-known. Solid lines show potentials as indicated, and dashed lines with the same color for the RDFs obtained with the same potential. (a) IBI results after 50 and 300 iterations (green and blue). (b) Final results obtained with an IBI variant (red) and with IMC (green). The true potential is best reconstructed with the IMC method. All potentials, however, yield RDFs that are almost indistinguishable from the target RDF. Data provided by David Rosenberger.

interaction sites.^{324,343,344} Scherer, Andrienko, and co-workers have developed systematic ways to derive such potential, either by force matching³²⁷ or by using kernel-based machine learning with covariant meshing in order to account for inherent symmetries.³⁴⁵ So far, this has only been applied for small molecules, but it also offers interesting perspectives for simulations of, e.g., semicrystalline polymers.

An alternative way of parametrizing strongly configuration dependent effective interaction potentials has recently been developed by Bereau and Rudzinski.^{346,347} Their idea is to use different CG force fields for different regions in (local) configurational space, and interpolate (“hop”) between them depending on the current state of the system. This multisurface concept, borrowed from models for electronic transitions, allows for a much better local optimization of force fields without having to resort to complicated force field parametrizations. As a nice side effect, potential barriers can also be represented much more accurately, which greatly improves the dynamic properties of the system. A related “multiconfigurational” concept designed to capture conformational chain transitions and their effect on potentials of mean force has been proposed by Sharp et al.³⁴⁸

III.A.2. Thermodynamics-Based Coarse-Graining. The coarse-graining approaches discussed in the previous section yield CG models that capture structural properties of the FG reference system such as pair correlation functions or statistical averages of mechanical force fields. From a multiscale point of view, it might often be more interesting to capture thermodynamic properties such as the equation of state (the density), the compressibility or more generally, high-wavelength structure factors, solubility parameters, interfacial tensions and surface tensions. Thermodynamics-based CG strategies are popular in top-down coarse-graining, as they use thermodynamic quantities as input which are more easily accessible in experiments. Typically, a certain functional form of potentials is assumed, and the parameters are matched such that the CG model reproduces the desired thermodynamic properties. For example, van der Haven et al.³⁴⁹ have recently derived a very accurate approximate closed-form expression for the coexistence phase diagrams of binary polymeric mixtures in DPD models with pair interactions, which allows to directly relate the soft DPD interaction parameters with experimental data on demixing phase behavior.

Thermodynamics-based coarse-graining is also the most natural approach when designing field-based continuum models or extremely CG models with soft potentials such as DPD or density-based potentials. As we have discussed above, density-based models and field-based continuum models are closely related to each other. There also exists a direct connection between DPD and continuum mechanics: For simple fluids, Español and Revenga have introduced a variant of DPD,³⁵⁰ termed “smoothed dissipative particle dynamics” (sDPD), which is entirely constructed from thermodynamic properties and can be seen as a Lagrangian solver for the fluctuating Navier–Stokes equations.

When constructing ultracoarse-grained models, one must again distinguish between bonded and nonbonded potentials. Bonded potentials can be determined in a structure-based manner as described in section III.A.1. On large scales, when studying polymers of large molecular weight, it is often sufficient to use simple chain models such as the discrete or continuous Gaussian chain model,¹⁸ which requires matching only one parameter (the Kuhn length for given number of Kuhn segments)³⁵¹ to the average conformational properties of the

chains in the reference system. Determining nonbonded interactions is more difficult, as standard density-based potentials or interaction terms in field-based models (eqs 2 and 5) are typically framed in a thermodynamic language in terms of compressibilities, Flory–Huggins χ parameters (eq 3) etc.

Specifically, mapping χ parameters still represents an outstanding challenge. Field-theoretic models typically assume that it describes the effective nonbonded interactions between CG polymer segments and is independent of local composition, chain length, and chain architecture. This picture is clearly greatly simplified and it has long been unclear whether the concept of a purely monomer-based χ parameters is at all reasonable. Luckily, recent work by Morse, Matsen and co-workers^{235,352,353} on diblock copolymer melts suggests that this is probably the case, at least for dense polymer melts, due to a universality in the phase behavior of polymers with large molecular weight. They proposed to determine the χ parameter in diblock copolymer melts by fitting the collective structure factor in the disordered state of symmetric diblock copolymer (BCP) melts to accurate theoretical predictions of a renormalized theory that accounts for the effect of fluctuations and finite chain lengths.³⁵⁴ Using this top-down mapping method, they were able to quantitatively reproduce the location of the order–disorder transition (ODT) in BCP melts of a number of particle-based models^{352,354} and also experimental systems³⁵³ after accounting for the effect of polydispersity. Building on this insight, Willis et al.³⁵⁵ proposed as alternative approach to directly use the ODT for mapping χ after correcting for effects of polydispersity and compositional asymmetry. Reanalyzing published experimental data, they mapped $\chi(T)$ onto the functional form

$$\chi(T) = \frac{A}{T} + B \quad (12)$$

where A subsumes enthalpic and B entropic contributions to the effective segment interactions, and extracted values of A and B for 19 different chemical pairs.

The χ -calibration scheme of Morse and co-workers relies on the existence of accurate theoretical predictions for the structure and phase behavior of diblock copolymer melts. When looking at more complex systems, such predictions are usually not available, and less accurate mapping procedures must be adopted. Theories of the χ -parameter have a long history, see, e.g., refs 356–364 (the list is far from complete). Practical mapping schemes for determining effective χ -parameters have been proposed already 30 years ago by Müller and co-workers^{365,366} and applied successfully to lattice models for polymer mixtures. In cases where the factors contributing to the χ -parameter are mainly enthalpic, Müller and Binder proposed, as a simple prescription, to determine an “effective coordination number” from interchain correlation functions,³⁶⁵ which replaces the coordination number in the original Flory–Huggins theory.^{367,368} Müller also devised a scheme to obtain additional entropic contributions from independent studies of the equation of state in “athermal” systems, where enthalpic interactions have been switched off.³⁶⁶ More recently, a number of heuristic schemes for matching Flory–Huggins type interaction parameters have been proposed by De Nicola and co-workers,^{369,370} that rely on either matching energies with CG off-lattice models³⁶⁹ or adjusting conformational properties of homopolymers in solution.³⁷⁰ Ledum et al. have developed a machine-learning protocol for optimizing such parameters with respect to

arbitrary target quantities, e.g., density profiles.³⁷¹ Sherck et al.³⁷² and Weyman et al.³⁷³ have recently developed systematic bottom-up coarse-graining strategies for deriving field-based models with nonbonded monomer interactions that are not restricted to the Flory–Huggins form (eq 3). Their idea is to proceed in two steps. In the first step, a CG particle-based with soft pair potentials of given functional form is determined from reference simulations of a microscopic model, e.g., by relative entropy minimization³⁷² or by matching the RDF. The second step is a Hubbard–Stratonovich transformation that turns the particle model into an auxiliary field model, which can then be studied by field-theoretical simulations. The second step involves an inversion of the pair potential in Fourier space, which restricts the class of potentials for which the approach can be applied.³⁷³ In particular, the inversion is not possible for hard core potentials, therefore the first step is essential and cannot be omitted. The latter still remains true if one replaces the Hubbard–Stratonovich transformation by a delta functional transformation in order to obtain a field theory of the type of eqs 4 and 5. Such an approach would give additional flexibility because higher order multibody interactions can be included.^{145,161,162} The underlying density-based potential does not have to be an integral over a local free energy density $f(\vec{r}, \underline{\rho})$, it could also describe nonlocal interactions as, e.g., in

$$U_{\text{nb}}[\underline{\rho}] = \frac{1}{2} \sum_{\alpha\beta} \iint d^3r d^3r' \rho_{\alpha}(\vec{r}) \rho_{\beta}(\vec{r}') V_{\alpha\beta}(\vec{r} - \vec{r}') \quad (13)$$

however, the integral over $V_{\alpha\beta}(\vec{r})$ still needs to exist and be finite. We should note that, strictly speaking, the bottom-up approaches of Sherck et al. and Weyman et al. use ideas taken from structural coarse-graining. Nevertheless, the resulting CG models do not capture local structural properties such as packing effects, hence they are closer to thermodynamically CG models than to structurally CG models.

Compared to structural coarse-graining, one disadvantage of thermodynamics-based coarse-graining is that one loses the direct connection between mechanical forces in the CG and the FG system. Since forces drive the dynamics, it becomes more difficult to restore the correct dynamical properties without further adjustments. Indeed, recent studies on ionic liquids³⁷⁴ have suggested that structure-based CG models tend to have a more consistent dynamical behavior than thermodynamically CG models, e.g., regarding the relative mobility of anions and cations. We will specifically discuss issues of dynamic coarse-graining in the next section. Thermodynamics-based coarse-graining also becomes questionable in systems far from equilibrium, e.g., in active fluids. One should note, however, that many structure-based coarse-graining techniques are also no longer applicable for such systems, as most of them—with the exception of force matching—assume local thermodynamic equilibrium: They assume local configurations to be Boltzmann distributed in subvolumes of size comparable to the correlation length.

III.B. Dynamic Coarse-Graining

The most common approach to studying dynamical properties in CG simulations is to use the free energy landscape obtained from a static equilibrium coarse-graining procedure as an effective interaction potential in molecular dynamics (MD) simulations. This approach can be quite successful if one accounts for a few side effects of structural coarse-graining: First, as known from the Mori–Zwanzig formalism²⁸⁷ integrating out degrees of freedom invariably introduces friction terms and

stochastic noise terms in the CG dynamical equations. In a standard MD simulation, these friction terms are disregarded, which accelerates the dynamics. Second, CG free energy landscapes are typically smoother than atomistic ones, which further reduces the direct friction between CG particles. As a result, coarse-graining reduces the separation between originally highly disparate time scales such as, e.g., the inertial and the diffusive time scales (the telescope effect),³⁷⁵ and accelerates slower dynamical processes.

From the point of view of time bridging, both the speedup and the telescoping are beneficial, as they allow one to access later time scales in CG simulations³⁷⁶ and study processes on different time scales simultaneously in one simulation. One of the earliest⁹⁶ and still widely and successfully used approaches to dynamic coarse-graining has been to simply take advantage of this effect, determine the speedup factor of the process of interest, and use this to map the CG dynamics on real dynamics,^{377–382} taking into account that the speedup factor might be different for different processes and/or components.³⁸⁰ However, care must be taken that the speedup does not change the order of “faster” and “slower” processes and which might change dynamical pathways, particularly in dynamically asymmetric systems. This defines the problem of *dynamic consistency*.¹²

As already discussed in the previous section, one key to reducing the dynamic consistency problem is accurate structural coarse-graining, as it helps to recover consistent dynamics even in standard MD simulations, i.e., consistent barrier crossing dynamics and consistent relative speedup.^{346,374} In fact, using kinetic information as additional input for the parametrization of coarse-grained force fields may improve their quality,^{383,384} because it gives more weight to transitional conformations, which are typically not well sampled in standard coarse-graining approaches. For instance, Xia, Keten and co-workers have recently proposed an “energy renormalization” method for adjusting the activation barriers in CG models of polymer glasses, which allows to recover the dynamical and rheological properties obtained from all-atom reference simulations over a wide temperature range.^{385–387}

In addition, one can manually reintroduce terms in the dynamical equations that mimic the effect of the interactions between the CG variables and the remaining “irrelevant” degrees of freedom, i.e., friction and corresponding stochastic noise³⁸⁸ and, possibly, memory.

III.B.1. Dynamic Rescaling. Gaining a more quantitative understanding of the dynamic speedup between FG and CG models is an interesting problem of statistical mechanics. One promising approach is excess entropy scaling. The idea goes back to the “principle of corresponding states” as formulated by Helfand and Rice in 1960,³⁸⁹ which states that, for fluids of particles interacting with a potential of the form $V(r) = \epsilon u^*(r/\sigma)$, the dynamical and transport properties for different σ and ϵ can be mapped onto each other. For that particular choice of potential, the correspondence can be shown by simple dimensional analysis and seems close to trivial, but it does establish an interesting correlation between dynamic and thermodynamic quantities. Building on this and a method to map simple fluids onto hard sphere fluids,³⁹⁰ Rosenfeld proposed a heuristic approach to identifying corresponding states in simple fluids based on their excess entropy,^{391,392} which turned out to be remarkably successful in both the dense and dilute limits. Recently, Rondina et al.³⁹³ have shown that excess entropy scaling can also be applied in dense polymer melts. They

used a simple bead spring model as a starting point which was coarse-grained to different degrees and showed that the ratio of dynamical quantities like the bond relaxation time τ or the viscosity η in the CG and FG system followed an exponential law

$$X_{\text{CG}}/X_{\text{FG}} = A \exp(\alpha \Delta S_{\text{exc}}) \quad (14)$$

in a wide temperature range (with $X = \tau$ or η). Here ΔS_{exc} is the temperature-dependent excess entropy difference between the CG and the FG system which was determined by thermodynamic integration. However, the correspondence was found to be less universal than one might hope, since both α and A depend on the CG model.

Lyubimov, Guenza, and co-workers^{394–396} have considered CG models that map polymer melts onto a fluid of interacting soft blob, and designed a first-principles approach that allowed them to estimate the speedup factor with remarkable accuracy. They assumed that the speedup factor has two contributions: The first is based on a simple rescaling according to the principle of corresponding states.³⁸⁹ The second accounts for the different environments of the interacting units, i.e., the different effective friction constants of monomers that are part of a tagged chain and of tagged CG particle in a melt environment. Both are calculated within mode coupling theory³⁹⁷ and then mapped onto each other. Using this ansatz, Guenza and Lyubimov were able to derive analytical expressions for the dynamic speedup factor of diffusion constants in chemically realistic melts such as polybutadiene.³⁹⁶ Unfortunately, the calculations require a rather involved analytic machinery, and extensions to complex inhomogeneous systems and mixtures are not yet available.

The dynamic rescaling approach can also be applied to nonequilibrium systems, e.g., sheared polymer fluids or amorphous polymer materials under extreme stress. Ge and co-workers have recently studied polystyrene glasses under shear, uniaxial compressive stress,³⁹⁸ and tensile stress which was strong enough to induce crazing.³⁹⁹ They compared the results of CG, united-atom (UA), and all-atom (AA) simulations using a simple rescaling prescription that targeted the stress tensor and found that a single rescaling factor was sufficient to (roughly) collapse the entire stress–strain curves of the different models. This was even true when looking separately at the conservative (elastic) and dissipative contributions to the total stress. In the case of crazing,³⁹⁹ they showed that the craze fibril structure was similar in the three models, and AA craze configurations could be reconstructed from CG simulations. This demonstrates that CG simulations can be used to accelerate simulations and access later times in simulations of non-equilibrium processes.

III.B.2. Introducing Friction. In particle-based CG models, natural frameworks for introducing friction are the Langevin thermostat, which allows to assign separate friction constants for every CG particle, or the DPD thermostat, which conserves momentum and allows to adjust independently the friction parameters for every pair of interacting CG beads.

A natural generic way to determine CG friction parameters from FG simulations is provided by the Green–Kubo formalism, which relates the friction force experienced by a particle moving at fixed velocity to the integral over the time correlation function of the fluctuating forces acting on the particle (the FAF). In the language of linear response theory, this expression relates a steady-state generalized “current” (in this case the mean force on the particle) building up in response to a constant “thermodynamic force” (in this case the fixed velocity) to the time-integrated current–current (in this case force–force) correla-

tions. Phrased in this way, one can immediately see why a naïve application of the approach to FG simulation trajectories is dangerous: The velocity of the CG particles is not fixed, instead it fluctuates and averages to zero, and as a result, the integral over the FAF vanishes as well.³⁸⁸ If the time scales of the dynamics of CG variables and remaining irrelevant variables are well-separated, one can overcome this problem by monitoring the running Green–Kubo integral as a function of an upper time cutoff. It will then first reach a more or less well-defined plateau before it starts decaying, and the plateau value can be used to extract values for the friction parameter.⁴⁰⁰ However, the choice of the time cutoff value remains somewhat heuristic.

One way to overcome this so-called “plateau problem” is to constrain the dynamics of the FG simulations such that the momentum of the CG particles is kept fixed. A corresponding bottom-up scheme for determining DPD friction parameters from FG simulations was first proposed by Akkerman and Briels³⁸⁸ and later derived more formally by Hijón et al.²⁸⁵ based on the Mori–Zwanzig formalism and an additional Markovian assumption. The idea is to modify the dynamics of the FG simulations such that the desired collective CG variables are constrained to fixed values and do not participate in the dynamics. This effectively decouples the FG dynamics from the CG dynamics and solves the plateau problem. Hijón et al.²⁸⁵ demonstrated the power of the approach using the example of star polymer melts, and several other authors have later applied it to derive CG DPD models for chemically realistic oligomers or polymers such as *n*-alkanes,⁴⁰¹ polybutadiene,⁴⁰² and dimethylpropane.⁴⁰³

III.B.3. Introducing Memory. The strategy of absorbing the full dynamics of the irrelevant variables in a single set of DPD friction parameters is justified if the time scales in the CG model are well separated from those processes in the FG system that have been integrated out.³⁸⁸ However, if the degree of coarse-graining is comparatively low, or if the CG model does not capture all slow processes in the FG model, the time scale separation of characteristic processes at the FG and the CG level is incomplete. In such cases, the Mori–Zwanzig projection technique²⁸⁷ yields CG dynamical equations that are non-Markovian, i.e., include memory terms. Two types of approaches have been adopted in the past to account for this effect.

The first is to introduce virtual, but physically motivated variables, which mimic the effect of slow processes that have been eliminated in the CG model,^{404,405} while not affecting the structural and thermodynamic properties of the CG system. One example is the slip links discussed in section II.C, which are introduced to restore the effect of entanglements, i.e., the slow dynamics of topological constraints that are removed in extremely coarse-grained models. Wu et al. have recently developed a systematic method to derive slip-link parameters from experiments or FG simulation data.¹⁹⁸ Another example is the RaPiD model for polymers developed by Briels and co-workers, which uses the center of mass of molecules as CG variables, but introduces a set of additional virtual variables that characterize the conformational state of the molecules.^{406,407}

The second approach is to cast the dynamical equations in the CG model in the form of generalized Langevin equations (GLEs), i.e., to explicitly include memory in the CG dynamical equations.¹⁴ Setting up such equations is a highly nontrivial task. In particle-based CG models, one would ideally like to use a multidimensional GLE of the type

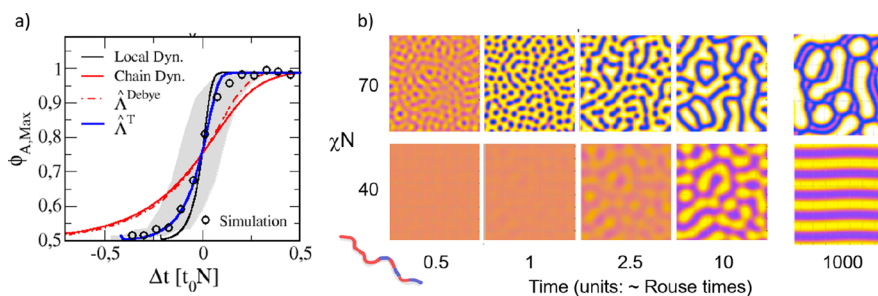


Figure 6. (a) Time evolution of order parameter in a diblock copolymer melt after a sudden quench according to different DDFT models (line) and CG particle-based simulations (symbols). The DDFT functional $\hat{\Lambda}^T$ that has been constructed from the particle model. Adapted from ref 220. Copyright 2020 American Chemical Society. (b) Snapshots during the ordering of a melt of two-scale multiblock copolymers ($A_{5n}B_nA_nB_nA_nB_n$ structure) after a sudden deep (top) and shallow (bottom) quench. Adapted with permission under a Creative commons CC BY 4.0 License from ref 221. Copyright 2020, Schmid/Li.

$$M_i \dot{\mathbf{V}}_i(t) = \mathbf{F}_i^C(t) - \int_0^t ds \sum_j \mathbf{K}_{ij}(t, s) \mathbf{V}_j(s) + \partial \mathbf{F}_i(t) \quad (15)$$

where M_i and \mathbf{V}_i are the mass and velocity of CG particles, $\mathbf{F}_i^C(t)$ and $\partial \mathbf{F}_i(t)$ the conservative and fluctuating stochastic forces acting on them, and $\mathbf{K}_{ij}(t, s)$ is a multidimensional memory kernel that depends on the configuration at time t and s , and which is related to the stochastic force by a fluctuation–dissipation relation

$$\langle \partial \mathbf{F}_i(t) \partial \mathbf{F}_j(s) \rangle = m_j \sum_k \mathbf{K}_{ik}(t, s) \langle \mathbf{V}_k(s) \mathbf{V}_j(s) \rangle \stackrel{\text{equil.}}{=} k_B T \mathbf{K}_{ij}(t, s) \quad (16)$$

Note that we have used a tensor notation here, and the last equality $\stackrel{\text{equil.}}{=}$ uses the relation $\langle \mathbf{V}_j(s) \mathbf{V}_k(s) \rangle = 1 \delta_{jk} k_B T / m_k$, which is valid at thermodynamic equilibrium. The form (eq 15) has been derived by Kinjo and Hyodo⁴⁰⁸ based on Mori–Zwanzig projections and additional approximations.^{17,286} The fluctuation–dissipation relation can also be derived from the Mori–Zwanzig projection operator formalism, but one can show that it is a general feature of GLEs which satisfy an orthogonality condition for the relation between random force and velocity.⁴⁰⁹ Several methods have been developed and analyzed that allow to determine memory kernels from FG simulations and thus construct GLE-based CG models in a bottom-up fashion.^{14,288,410–424}

The main practical problem with the CG equation, eq 15, is that simulations of such high-dimensional coupled integro-differential equations are computationally very time-consuming, mostly due to the high costs associated with generating the multidimensionally correlated noise that satisfies the fluctuation–dissipation relation. Therefore, simplifications must be made. The simplest and most efficient one is to ignore all cross-memory terms and replace $\mathbf{K}_{ij}(t, s)$ by a single scalar function, $\mathbf{K}_{ij}(t, s) = 1 \delta_{ij} K(t - s)$. This approach has been used, among others, by Wang and co-workers^{420,425} to model polymers in dilute solution and by Klippenstein and van der Vegt to model polymer melts.⁴²² In their approach, Klippenstein van der Vegt explicitly address the issue of multibody correlations and propose a method to replace them by a single effective self-memory kernel. To this end, they introduce a new scheme for consistently including the cross-correlations between the stochastic forces and the conservative interactions with the

effective medium, which turns out to be quite accurate in their studies of star polymer melts⁴²² and Asakura–Oosawa fluids.⁴²⁴

Going beyond pure self-memory kernels, Li and co-workers have suggested an approach, termed “non-Markovian DPD” (NM-DPD), which decomposes the memory kernel into a sum of frequency dependent DPD friction functions.^{426–428} This relieves the noise generation problem, as the stochastic forces can then be decomposed in the same pairwise manner. Unfortunately, the approach puts severe constraints on the self-memory part of the memory-kernel \mathbf{K}_{ii} , since it assumes $\mathbf{K}_{ii} = -\sum_{j \neq i} \mathbf{K}_{ij}$. This can cause problems, e.g., when considering hydrodynamic interactions between CG particles in implicit solvent,⁴¹⁶ or diffusion of molecules in penetrant networks.⁴⁰³ To overcome the problem, Jung et al. have developed a more general scheme for reconstructing and treating pair memory kernels that decouples self- and pair-friction while still ensuring linear scaling for short-ranged pair-interactions.⁴¹⁶

When comparing the two approaches to account for memory in CG systems—physically motivated virtual variables and GLE-based CG models—we should note that the practical solution of GLE equations also often involves the use of auxiliary variables.¹⁴ However, these auxiliary variables are just introduced as a numerical trick to solve the GLE and have no physical meaning.^{280,429–433} The idea is to replace the GLE by a set of regular Langevin equations in an extended phase space. This is possible if the memory kernel can be approximated by a finite sum of possibly complex, but decaying exponentials (a Prony series).⁴³⁴ Alternatively, the parameters of the Langevin equations can be determined directly from correlation functions obtained in FG simulations^{420,421} in a numerically well-controlled manner.⁴²¹

III.B.4. Transition Particle-Continuum. So far, we have discussed dynamical coarse-graining issues in particle-based models. Closely related problems arise in dynamical coarse-graining from particle to continuum equations, when the CG equations are dynamic equations for continuous fields. If the fields describe complex fluids, e.g., polymer systems, one again needs to account for a multitude of time scales^{435–438} which often precludes the use of, e.g., simple Cahn–Hilliard type equations.⁴³⁹ Wang et al.²²⁸ have considered dynamic density functional (DDFT) equations of the type (eq 6), but with the mobility function replaced by a time-delayed memory function $\Delta(\vec{r} - \vec{r}'; t - t')$, which they calculated analytically in random phase approximation. They studied the effect of memory on the ordering/disordering kinetics in homopolymer and block copolymer melts and found very good agreement between particle-based simulations and continuum simulations.²²⁸ One

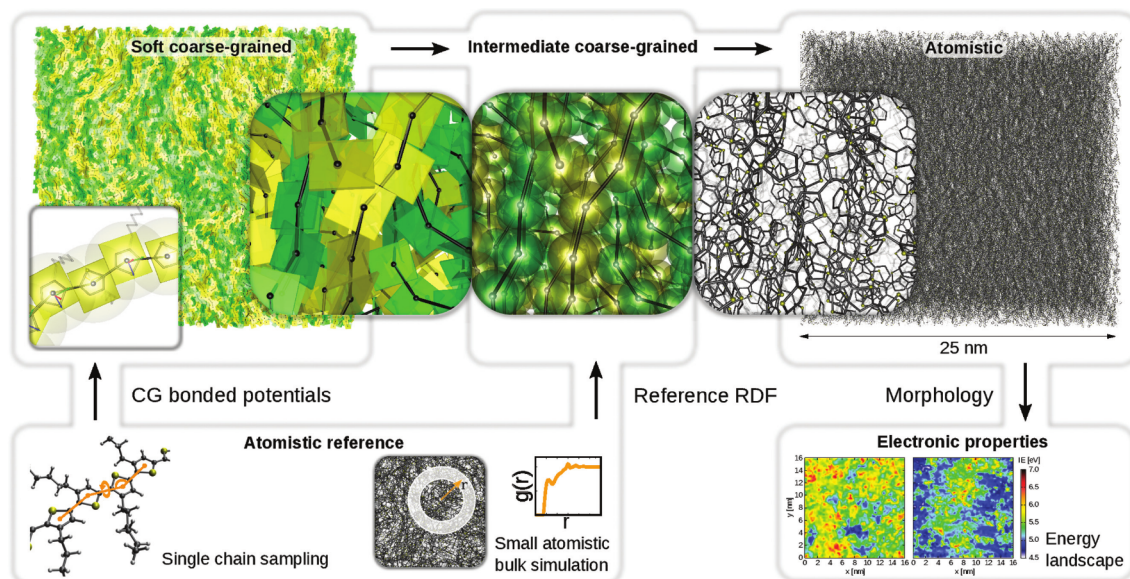


Figure 7. Multiscale strategy for predicting charge transport in polymeric semiconductors.⁴⁷⁸ See text for explanation. Reproduced with permission from ref 478. Copyright 2015 John Wiley and Sons.

key to success in such an approach is to identify the appropriate CG collective variables (densities). Very recently, Müller analyzed this problem⁴⁴⁰ by examining three situations where seemingly identical initial density perturbations were created in different ways, first by applying a modulated force on all segments of a melt, second by applying a force on end segments only, and third by applying a force on a selected middle segment. In particle-based simulations, the dynamic response to these perturbations was found to be very different in the three cases. This could be reproduced in the continuum simulations if the densities of segments which had experienced the initial force and those of passive segments were treated as separate collective variables.

From the point of view of dynamic coarse-graining, polymers have the convenient feature that relaxation processes on different time scales can often roughly be associated with different length scales. Therefore, Markovian DDFT models such as eq 6 may be able to capture the multiscale dynamics if the nonlocal mobility matrix function is adjusted properly $\Delta(\vec{r} - \vec{r}')$. Mantha et al.²²⁰ developed a bottom-up method to construct $\Delta(\vec{r} - \vec{r}'; t - t')$ from reference FG particle simulations and found that simulations based on the resulting DDFT model are in very good agreement with corresponding particle-based simulations (see, e.g., Figure 6). Matching mobility matrices is also a convenient way to map different CG particle-based polymer models onto each other.⁴⁴¹

One should note, however, that these approaches are restricted to systems close to equilibrium. Far from equilibrium, a CG continuum description operating with densities only is certainly not sufficient and one needs to introduce additional variables that characterize the chain conformations.⁴⁴² Furthermore, polymer stretching generates mechanical stresses, therefore, the use of a purely diffusive dynamical model such as eq 6 (model B dynamics) is no longer justified. An appropriate CG model in such cases must also include momentum and hydrodynamics. As we have discussed in section II.E, viscoelastic models are quite commonly constructed from molecular polymer models such as the elastic dumbbell model. Up to now, this is mostly based on analytical considerations using

substantial mean-field approximations, and to the best of the author's knowledge, systematic bottom-up strategies to construct full viscoelastic models from FG simulations are still missing. So far, coarse-graining strategies that connect particle models with continuous viscoelastic models for polymeric fluids are mostly based on parameter mapping.²⁷¹ This also holds for elastoplastic models for polymeric glasses.⁴⁴³

Alternatively, it is sometimes possible to combine multiscale approaches with theoretical insights, e.g., from the tube model of viscoelasticity, in order to answer specific questions. One example of such a theoretically informed scale bridging scheme is the branch-on-branch algorithm by McLeish and co-workers.^{444,445} It builds on a theory for the rheology of branched polymers, the so-called pom-pom model by Bishko et al.,⁴⁴⁶ which estimates the relaxation modulus of chains for given polymer architectures, requiring only a few additional input parameters. The branch-on-branch algorithm establishes a connection between microscopic simulations of the synthesis of highly branched polymers and their rheological properties. The microscopic simulations are used to generate a representative sample of branched polymers, which are then fed into the theoretical machinery. The method was applied successfully by Read et al. commercial Low density polyethylene (LDPE), and recently by Zentel and co-workers to predict the rheological properties of LDPE and polybutyl acrylate (PBA) from the reaction conditions in a miniplant.^{447–451}

III.B.5. Accessing Late Times. So far, we have mainly discussed strategies to infer correct and consistent dynamical properties from CG models. However, even though CG simulations can cover much longer time spans than atomistic simulations, this is usually not sufficient to access experimentally relevant time scales of seconds, minutes, or even months. In order to do so, one must also coarse-grain in time.

In situations when it is possible to identify single activated events that slow down the time evolution of a system, one can resort to rare event sampling techniques. Typical problems that are considered with such approaches are, e.g., refolding events of molecules or nucleation processes in materials. A large portfolio of methods has been proposed to study them,⁴⁵² such as

weighted ensemble techniques,^{453,454} transition path sampling,^{455–457} forward flux sampling,^{458–460} the string method,^{461,462} or a combinations thereof.⁴⁶³ Using such methods, one can extract rate constants that can be fed into a kinetic model in order to simulate a system on larger time scales.

More generally, one of the most powerful frameworks for coarse graining in time is Markov state modeling, which has become very popular in the field of biomolecular simulations.^{464–467} In Markov state models (MSMs), the configurational space is partitioned into many regions, called macrostates, and the dynamics is modeled in terms of a master equation by memory-less transitions between these states. The number of macrostates is typically chosen quite large, much larger than, e.g., the number of known metastable configurations of a system. Replacing the original molecular dynamics equation by such a relatively fine-grained Markovian process thus represents a severe approximation. In reality, the transitions between macrostates usually have some memory of the past. Nevertheless, it can be shown that for optimized mappings, the long-term dynamics is still reproduced very accurately by the MSM, as long as it is governed by a few dominant slow time scales.⁴⁶⁶

Currently, Markov state modeling is a well-established technique with solid theoretical foundations.⁴⁶⁶ Techniques are available how to optimize the partitioning into macrostates,⁴⁶⁸ how to determine transition rates and the associated uncertainty,⁴⁶⁹ and even how to use MSMs to connect theoretical models to experimental trajectory data.⁴⁷⁰ Recent machine learning based approaches offer additional opportunities for further optimization.^{471,472} Many of these techniques assume equilibrium; i.e., they require transition rates to fulfill detailed balance. Knoch and Speck have recently considered nonequilibrium MSMs (NE-MSM)s for driven systems^{473–476} and shown how to connect MSMs at different CG levels (i.e., with different microstate numbers) in a thermodynamically consistent manner. Knoch et al. also applied the MSM approach to the nonequilibrium problem of force-driven molecule unfolding and showed that MSMs can be used to bridge between loading rates in simulations to experimentally accessible loading rates.⁴⁷⁷

III.C. Multiresolution

The ultimate vision of multiscale modeling is to study the properties of a system simultaneously on different scales. Often, it is sufficient to establish one-way communication channels between simulations at different CG level. As an example of such a scheme, Figure 7 shows a strategy to predict the electronic transport properties of polymeric organic materials, which has been developed by Andrienko, Daoulas, and co-workers.^{170,478,479} It relies on a theoretical framework that relates the charge transport in organic semiconducting polymers to their local atomistic conformations,^{480–483} based on the Marcus theory of electron transfer rates.⁴⁸⁴ In the multiscale approach of Andrienko, Daoulas, and co-workers, coarse-grained and ultracoarse-grained force fields for conjugated polymers are constructed from atomistic reference simulations and (regarding the nonbonded interactions in the ultracoarse grained models) phenomenological considerations. Ultracoarse-grained simulations using these force-fields are then carried out to sample large scale morphologies, which serve as starting point for creating atomistic configurations by a successive backmapping strategy (see below). From the atomistic structures, a local ionization energy landscape is constructed, which allows to infer electronic properties such as the charge mobility.

This work flow demonstrates the power of multiscale approaches; however, it does not yet allow to account for possible feedback mechanisms between processes on different scales. One way to include them is provided by the “heterogeneous multiscale” (HMM) framework proposed by E and Engquist in 2003.⁴⁸⁵ The idea is to couple a macroscopic continuum simulation—in their case a fluid dynamics simulations—with microscopic FG simulations, which serve to estimate missing data for the macroscale model on the fly.^{486–489} The approach has recently been applied by Lukáčová-Medvid'ová and co-workers to study non-Newtonian flows of shear-thinning polymers melts in complex geometries.^{490–492} The HMM idea can also be extended to other types of continuum models. For example, Honda and Kawakatsu⁴⁹³ and Müller and Daoulas⁴⁹⁴ have proposed related mixed-resolution models that concurrently couple time-dependent Ginzburg Landau (TGL) models of (co)polymer blends to more detailed models of the same system: The long-time evolution of the composition profiles is simulated by TGL simulations, but SCF calculations⁴⁹³ or particle-based simulations⁴⁹⁴ are carried out intermittently, using the current TGL conformation as a basis, to readjust the parameters of the TGL model.

In some situations, it may be desirable to study large portions of a system with a coarse-grained model, but be able to zoom into selected regions in space with higher resolution. This concept goes back to the famous quantum mechanical/molecular mechanics (QM/MM) method⁴⁹⁵ by Warshel and Levitt, which combines electronic structure calculations in selected regions of space with classical atomistic molecular dynamics in the rest of the system, separated by a hybrid transition region. In a similar spirit, Prapotnik, delle Site, and Kremer in 2005⁴⁹⁶ and de Fabritiis, Delgado-Buscalioni, and Coveney in 2006⁴⁹⁷ have proposed mixed resolution dynamical simulation schemes for complex fluids that allow zooming into selected regions of space and studying them at higher resolution—the “AdResS” scheme⁴⁹⁶ and the “hybrid MD” scheme.⁴⁹⁷ Both, however, differ from QM/MM approaches or related approaches involving a CG outer region⁴⁹⁸ in one important aspect: They allow for a particle exchange between the CG and FG regions. The AdResS scheme⁴⁹⁶ achieves this by implementing a gradual switch between FG and CG force-fields in a transition region—or, in a later “Hamiltonian-AdResS” variant,⁴⁹⁹ a switch between interaction potentials. The hybrid-MD scheme⁴⁹⁷ couples a particle model to a continuum model via flux boundary conditions and allows to generate and remove particles in the transition region. The approaches have subsequently been refined and extended in various directions,^{500–502} combined with each other,^{503,504} and related schemes have been proposed. For example, Qi et al. have developed a scheme that couples field-based and particle-based polymer models^{505–507} via a spatially varying semigrandcanonical potential that enforces identity switches.⁵⁰⁸ As an interesting new idea for AdResS, Heidari and co-workers^{509–511} recently proposed to use an ideal gas as outer medium. While the latter hardly qualifies as a high-level model of a complex soft material, the setup allows one to carry out simulations with true open boundaries, to determine absolute free energies for the coupled FG system, and to enforce nonequilibrium situations with, e.g., steady-state currents.⁵¹⁰

A crucial component of many multiresolution schemes is backmapping: To connect different levels of resolution to each other, one must not only go up the scales by coarse-graining but also be able to go down, i.e., generate representative microscopic

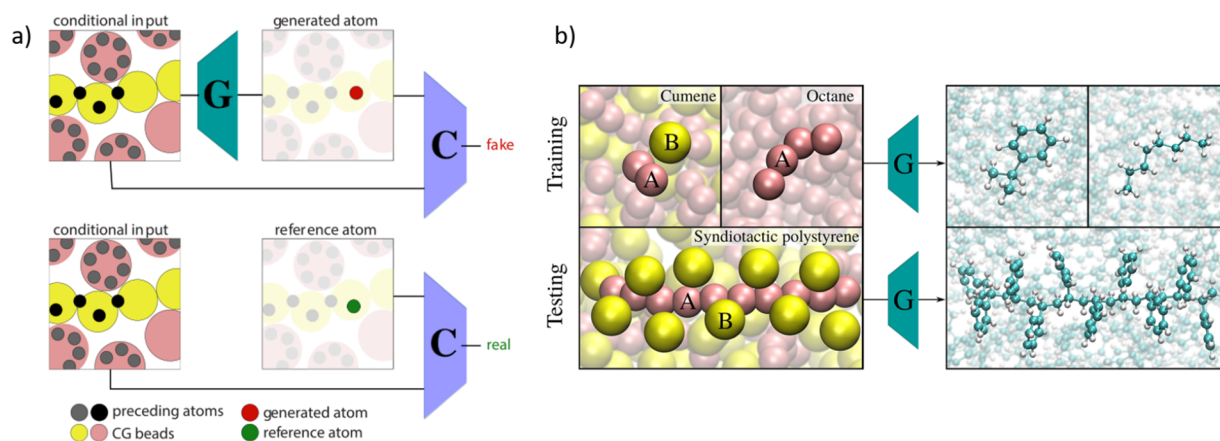


Figure 8. Backmapping strategy for polymer melts based on generative adversarial networks (GANs). (a) Sketch of the approach: A generator network G sequentially samples atom positions depending on the CG structure and the existing atoms. The discriminator C evaluates true and fake configurations based on the discrepancy between the positions of reference atoms and generated atoms. The training objective of G is to fool C , and the training objective of C is not to be fooled. Reprinted with permission under a Creative Commons CC BY 4.0 License from ref 512. Copyright 2020 Stieffenhofer/Wand/Bereau. (b) A GAN trained on cumene and octane can be used for backmapping of syndiotactic polystyrene. Reprinted with permission under a Creative Commons CC BY 4.0 License from ref 513. Copyright 2021, Stieffenhofer/Bereau/Wand.

molecular conformations from CG configurations. This is often done in a two-step procedure: First, some heuristic method is used to construct a first guess for the positions of the FG particles, and then, the FG configuration is further optimized by simulated annealing or another energy minimization method.^{97,377,514–516} Liu et al. have proposed an alternative method based on configurational bias Monte Carlo.⁵¹⁷ The backmapping problem is particularly challenging in the case of proteins, due to their complex chemical structure, and a number of sophisticated methods have been developed for this community. An overview can be found in ref 518, Table 3. Currently, machine learning tools borrowed from computer graphics become increasingly attractive. The reason is that the backmapping problem has some similarity with typical problems in computer graphics, such as filling a given rough frame with a representative set of textures. Stieffenhofer et al.^{512,513} and Li et al.⁵¹⁹ have recently developed backmapping methods based on deep generative adversarial networks (GANs), a framework where two neural networks—a “generator” and a “discriminator”—compete with each other in order to learn the main statistical properties of a training set in an unsupervised manner. Stieffenhofer et al. tested their scheme on syndiotactic polystyrene and showed that it can create good backmaps already before energy minimization, and that it is transferable: A GAN trained on melts can be used for backmapping of polymer crystals and even chemically similar (small) molecules^{512,513} (see Figure 8).

An interesting application of multiresolution tools is the generation of equilibrated polymer melt configurations for large molecular weight—which is still a difficult problem in polymer simulations.⁵²⁰ In traditional approaches, one first prepares a reasonably random initial configuration, e.g., by assembling a number of polymers with typical melt configurations, and then further relaxes it by implementing unphysical dynamics and/or Monte Carlo moves that allow chain crossing or even change chain connectivity.^{521–528} In multiscale approaches,^{529–536} one uses CG simulations to equilibrate the melt and then reconstructs a FG configuration by increasing the level of resolution in a stepwise fashion. Tubiana et al. have recently performed a systematic comparison of a traditional and a

multiscale equilibration scheme, focusing on topological indicators such as knot distributions,⁵³⁷ and found excellent agreement.⁵³⁸

III.D. Machine-Learning Based Strategies

Regarding virtually all aspects of scale bridging techniques discussed above, machine-learning (ML) based methods are becoming increasingly important.¹⁰² Kernel-based techniques or artificial neural networks (ANNs) are used for identifying suitable CG variables,^{472,539} for determining accurate atomistic potentials that bridge between ab initio calculations and standard classical force fields^{278,540} as well as for deriving improved coarse-grained potentials,^{15,306,328,339,345,541,542} for determining memory kernels from FG simulations,⁴²⁰ for constructing MSMs,^{471,472} or for backmapping.^{512,513,519} In some cases, ANNs can be trained to predict the outcome of CG simulations, such as, e.g., the conformation of heteropolymers for a given monomer sequence,⁵⁴³ the equation of state of homopolymer melts for given pair potential,³⁰⁶ or even complex quantities such as drug-membrane insertion free energies.⁵⁴⁴ This opens interesting perspectives for new coarse-graining strategies or new strategies of materials design.

Traditionally, an important application of ML in polymer science has been to predict material properties of interest of polymer based materials or composites, such as, e.g., the tribological properties, wear resistance, thermal conductivity,^{16,545–548} or even self-assembly.⁵⁴⁹ Specifically, ANNs have been used for some time to predict the glass transition temperature T_g , using as input either the chemical structure only^{550–553} or additional information from small-scale quantum mechanical calculations.^{554,555} Depending on the materials, the predictive power can be quite high.^{556–564} Such approaches can be applied, e.g., for identifying promising candidates for “high temperature polymers”⁵⁶⁵ with high T_g . More generally, a central vision in the emerging field of polymer informatics^{543,566–569} is to provide ML tools for the discovery of new interesting polymer materials. Ramprasad and co-workers have recently launched a polymer informatics platform (www.polymergenome.org) which offers tools for predicting a variety of polymer properties that include the density, T_g , the melting

temperature, the dielectric constant, the tensile strength, and many others.^{570,571}

One should note that, in general, extracting new physical insights from ML-based scale bridging strategies is not a trivial task. They can help to unveil hidden structure–property relations or correlations between different material properties,^{558,572} but they do not necessarily explain the underlying mechanisms. When used for coarse-graining and force field generation, they can be viewed as being a sophisticated interpolation scheme between available (training) data, but they do not necessarily help to understand general principles of coarse-graining or general features of CG models. On the other hand, feeding in theoretical knowledge of physical principles enhances the efficiency of ML-based procedures and reduces the amount of necessary training data.¹⁰² The resulting ML-based models usually have much higher predictive power than the original purely knowledge-based models. Hence knowledge-based and ML-based approaches to scale bridging and multiscale modeling mutually fertilize each other and should be seen as complementary.

IV. CHALLENGES FOR THE FUTURE

Comparing the available scale-bridging techniques in the last section to the examples of scale-bridging phenomena in polymers in the introduction, it becomes clear that we still need to go a long way before these two ends meet. Being able to gain a comprehensive quantitative understanding of real-world phenomena that includes the interplay of structures processes on all relevant scales, from the smallest to the largest, remains a grand challenge of polymer science. Several hard problems still need to be solved.

Strong Inhomogeneities. Real polymeric materials are usually multiphase materials, they are filled with internal interfaces, and their composition varies dramatically in space. Therefore, the transferability issues that still afflict most CG models represent serious problems that need to be overcome, e.g., by further improving coarse-graining strategies or by linking different CG models to each other in a multiresolution sense.

Defects. Defects are omnipresent in soft materials. They can be defined as very dilute and strongly localized perturbations that may come in several flavors.⁵⁷³ As doping defects in the form of local impurities, as connectivity defects that distort the local molecule structure, or as topological defects that do not involve any local chemical modifications, but still locally perturb the structure in a manner that they cannot be removed without global rearrangements of the whole system (examples are dislocations). Because they are highly dilute, they are usually not present in small scale simulations unless forced to be there; nevertheless, they tend to have a large and long-range impact on the material properties. In order to study this, small scale simulations should thus capture the effect of a defect that they actually do not contain, and that imparts its presence only, e.g., via nonperiodic boundary conditions.

Nonequilibrium and Processing. As discussed above, many traditional CG concepts are developed for equilibrium systems or at least build on a local equilibrium assumption. On the other hand, already the example of viscoelastic phase separation shows that in polymers, local equilibrium cannot be taken for granted even in seemingly simple problems such as spinodal phase separation. Most polymeric materials never reach equilibrium and their properties crucially depend on the way they have been created.³⁵ Therefore, quantitative multiscale descriptions must be able to account for processing pathways. The practical

importance of nonequilibrium processes in polymer systems has been acknowledged for a long time, and nonequilibrium phenomena as occur, e.g., in polymer rheology, have been a research focus since the beginnings of polymer science. Nevertheless, systematic scale bridging strategies for non-equilibrium polymers are still in their infancy.

Accessing Late Times. The time bridging strategies discussed in section III.B.5 have mostly been applied to single molecules or simple small systems and not to materials. In order to understand the properties of polymeric materials at late times, depending on environmental conditions, and to investigate phenomena such as aging, abrasion and wear, failure, and fatigue, one must account for all factors listed above (inhomogeneities, defects, processing history) and study their (co)evolution over a very long time period. So far, theoretical models^{574–576} are mostly based on empirical theories and with little connection to microscopic simulations.

Multiscale modeling of polymers thus remains a difficult problem, but it also offers exciting new prospects for the future. For instance, one fascinating challenge will be to develop systematic multiscale strategies for truly nonequilibrium living polymeric systems as are common in biology, which depend on strongly fluctuating local compositions and are constantly driven out of equilibrium.

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Notes

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