

Domain-wall induced large magnetoresistance effects at zero applied field in ballistic nanocontacts

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We determine magnetoresistance effects in stable and clean permalloy nanocontacts of variable cross-section, fabricated by UHV deposition and in-situ electromigration. To ascertain the magnetoresistance (MR) effects originating from a magnetic domain wall, we measure the resistance values with and without such a wall at *zero* applied field. In the ballistic transport regime, the MR ratio reaches up to 50% and exhibits a previously unobserved sign change. Our results can be reproduced by recent atomistic calculations for different atomic configurations of the nanocontact, highlighting the importance of the detailed atomic arrangement for the MR effect.

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The magneto-transport properties of a device change drastically when the dimensions become comparable to characteristic length scales, such as the mean free path, the Fermi wavelength or the exchange length [1], and nanocontacts offer the possibility to study such length scales. Furthermore, magnetic nanocontacts can accommodate geometrically confined magnetic domain walls (DWs) as the wall width scales with the constriction width [2]. In the smallest possible (i.e. atomic) contacts, this eventually leads to atomically abrupt spin structure changes.

In such narrow DWs the spins of the charge carriers can no longer adiabatically follow the spin structure direction. Consequently, significant magnetotransport effects have been predicted [3–5] and observed [6–9], opening also the prospect of novel device applications [10]. However, reliable magnetoresistance (MR) measurements on nanocontacts necessitate particular requirements in terms of stability, cleanliness and control of the spin structure. These requirements have previously been unattainable [11, 12] leading to the observation of artifacts such as magnetostriction [6, 13, 14] and contamination [15, 16].

In this Letter we report the first observation of large domain wall magnetoresistance (DWMR) effects up to 50% at *zero* field in exceptionally clean and stable permalloy (Py = Ni₈₀Fe₂₀) nanocontacts of tailored geometry [17]. In addition, the MR exhibits a previously unobserved sign change in the ballistic transport regime. This result can be reproduced by recent theoretical calculations highlighting the importance of the detailed atomic arrangement for the sign and magnitude of the MR [18].

The MR is measured at *zero* applied field in nanocontacts that are rigidly attached to a substrate [19]. Using a special device geometry, we control the spin structure and in particular the presence of a DW. Furthermore, the nanocontacts are fabricated and characterized at low temperatures in the same ultra-high vacuum (UHV) chamber without breaking the vacuum [20]. *In situ* electromigration allows us to reduce the cross-section of the nanocontacts in a controlled fashion during the study [21]. Using this unique approach, we study the MR in magnetic nanocontacts from the diffusive to the ballistic transport regime while minimizing artifacts due

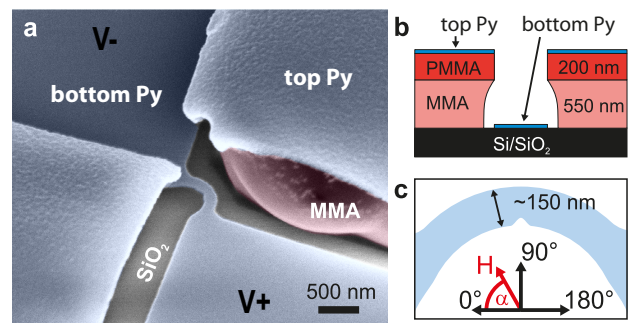


FIG. 1. (Color online) Scanning electron microscope image (viewing angle 45°) showing the constricted ring section before electromigration (blue: Py, red: resist, gray: SiO₂). The deformation of the MMA/PMMA resist is caused by the electron beam of the SEM. (b) Schematic illustration of the cross-sectional view of the sample and (c) the top view of the ring section indicating the orientation of the in-plane magnetic field angle α .

59 to magnetostriction and impurities.

60 After ex-situ fabrication of separated 5 nm Ti / 50
 61 nm Au contact pads on a Si/SiO₂ substrate, a double
 62 layer resist mask was defined by electron beam lithog-
 63 raphy (see Fig. 1(b)). Then the sample was mounted
 64 on a chip carrier and the Au pads were electrically con-
 65 nected by wire bonding. In order to keep the contacts as
 66 clean and stable as possible all subsequent steps (i.e. de-
 67 position, electromigration and MR measurements) were
 68 carried out in-situ in the same ultra-high vacuum (UHV)
 69 chamber [20] with a base pressure of $3 \cdot 10^{-10}$ mbar. A
 70 24 nm thick Py film was deposited onto the sample us-
 71 ing thermal evaporation. The resulting patterned film on
 72 the SiO₂ surface (see Fig. 1(a)) connects the pairs of Au
 73 pads thus allowing for electrical characterization of the
 74 structure. Due to the large undercut along the edges of
 75 the resist, the contacted film is electrically isolated from
 76 the Py deposited on top of the resist, as can be seen in
 77 Fig. 1(a) and 1(b). To study the MR effects associated
 78 with DWs, we have chosen a magnetic half ring structure
 79 with a constriction at its center (shown in Fig. 1(a,c)).
 80 In this geometry, DWs can be positioned precisely and
 81 reproducibly using a rotatable in-plane magnetic field H
 82 (Fig. 1(c)) [22].

83 To obtain nanocontacts of different cross-section, we
 84 carry out successive automated electromigration of the
 85 half-ring wire. Electromigration is widely used to form
 86 constrictions with contacts down to the ballistic trans-
 87 port regime with quantized conduction [7, 21]. The
 88 constriction defines the position of the highest current
 89 density in the structure and it hence determines where
 90 electromigration sets in. A typical measurement cycle
 91 consists of electromigration, where the constriction is
 92 thinned, followed by the in-situ characterization of the
 93 MR [19]. As the constriction is thinned, it quickly starts
 94 to dominate the overall resistance. It is hence primarily
 95 the MR response of this area which is probed by the MR
 96 measurements. Both electromigration and MR measure-
 97 ments are performed in UHV at a temperature of 80 K.
 98 This drastically reduces thermal noise and allows us to
 99 obtain mechanically stable contacts, which is not possi-
 100 ble at room temperature. The electromigration process
 101 is repeated until the contact is completely open, i.e., a
 102 gap has formed at the position of the constriction result-
 103 ing in an open circuit. Due to the increased noise and
 104 reduced stability of the contacts in the tunneling regime
 105 above $R > 50$ k Ω , we concentrate on stable resistances
 106 below that in the ballistic conduction regime. In this
 107 fashion we efficiently determine the evolution of the MR
 108 as a function of contact resistance, minimizing artifacts
 109 due to magnetostriction and impurities.

110 Three different types of measurement were employed
 111 to study the MR effects associated with DWs. The resis-
 112 tance of the contacts was measured (i) as a function of
 113 applied field angle α (see Fig. 1(c)) for a given applied
 114 field amplitude to determine the AMR, (ii) as a function

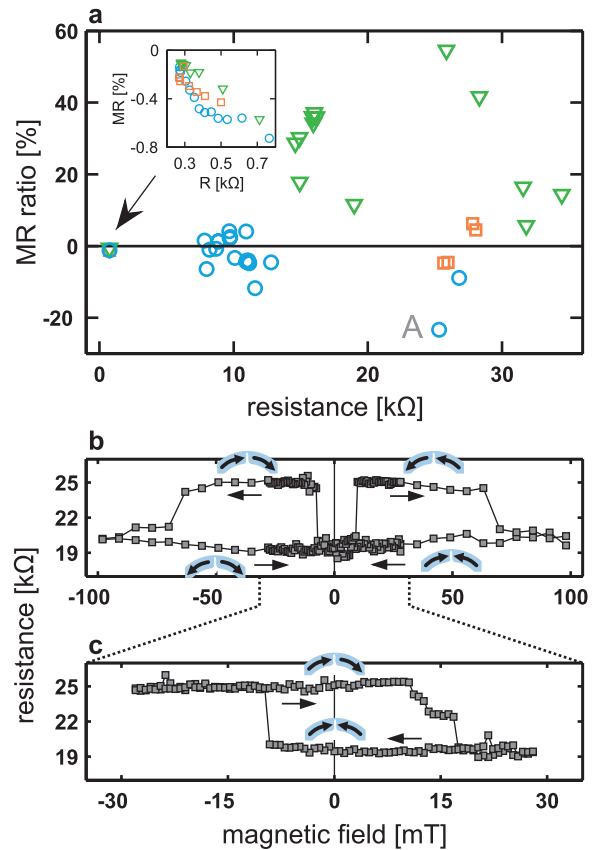


FIG. 2. (Color online) (a) Magnetoresistance ratio $MR = (R_{AP}R_P)/R_P$ vs. contact resistance in the parallel state (R_P) for three nanocontacts (blue, green and red). The data points are acquired from $R(H)$ loops with $\mu_0 H_{max} = 100$ mT and $\alpha = 75^\circ$ and 90° . The inset shows the evolution of AMR for low contact resistances at the beginning of the electromigration process. Resistance vs. magnetic field (b) major and (c) minor loop at field angle $\alpha = 75^\circ$ for the contact state labeled 'A' in Fig. 2(a). The sketches of the half-ring structure illustrate the magnetization configuration of the contact leads for different positions in the loop. The black arrows along the curve indicate the sweep direction.

115 of the field amplitude for a given field angle α ($R(H)$ -
 116 loop) and (iii) as a function of field angle α at remanence
 117 after applying a magnetic field along α and reducing the
 118 field to zero (for details on (iii), see the quasi-static mea-
 119 surement scheme in Refs. 19 and 22). In the following,
 120 the MR ratio is defined as $(R_{AP} - R_P)/R_P$, where R_P
 121 and R_{AP} denote the resistance of the nanocontact with
 122 both arms of the half-ring oriented in a parallel (P state,
 123 no DW) and anti-parallel (AP state, DW at the constric-
 124 tion) configuration, respectively.

125 In agreement with our previous findings [19, 22], we ob-
 126 serve different resistance levels with and without a DW
 127 pinned at the constriction in both the diffusive and the
 128 ballistic regime. The switching between these states is
 129 illustrated in Fig. 2(b): We first measure the MR for

130 a field of 100 mT applied approximately along the di-
 131 rection of the constriction ($70^\circ < \alpha < 110^\circ$) with the
 132 magnetization aligned along the angle α . After removing
 133 the field, the spin orientation is determined by the shape
 134 anisotropy of the narrow structure causing the spins to
 135 align parallel to the edge. A head-to-head DW is formed
 136 at the constriction, associated with a resistance value of
 137 the nanocontact of $R_{AP} \sim 19$ k Ω . When the field is
 138 reversed, the magnetization configuration changes to a
 139 quasi-single domain state without a DW ($R_P \sim 25$ k Ω)
 140 [22]. At higher reversed field, a new DW is nucleated.

141 Initially, all of the nominally identical samples exhibit
 142 a resistance of ~ 275 Ω (Fig. 2(a)). For such low resis-
 143 tance values the MR is dominated by anisotropic magne-
 144 toristance (AMR) with a magnitude of approximately
 145 1% [19]. Up to $R_P \approx 1$ k Ω , the MR gradually increases
 146 due to the growing contribution of the constriction resis-
 147 tance to the total resistance. As discussed in our ear-
 148 lier study [19], the MR behavior of nanocontacts in this
 149 low resistance regime can be entirely explained by the
 150 bulk AMR effect. In contrast to what has been reported
 151 elsewhere [7], we do not observe any sign of measurable
 152 DWMR in this low resistance regime.

153 Next we turn to the ballistic conduction regime above
 154 ~ 5 k Ω , where novel MR effects are expected to oc-
 155 cur. As the diameter of the magnetic nanocontact ap-
 156 proaches atomic dimensions, thermal and electromigra-
 157 tion effects can lead to significant rearrangements on the
 158 atomic scale, changing the total resistance of the con-
 159 tact. In contrast to the low resistance regime, the resis-
 160 tance changes during electromigration occur as distinct
 161 steps between stable levels as well-defined atomic recon-
 162 figurations take place at the narrowest part of the contact
 163 [21]. The MR changes significantly in this atomic contact
 164 regime. Its magnitude increases to more than 50% (Fig.
 165 2(a)) and we observe positive and negative MR. This
 166 large MR effect completely supersedes the small AMR
 167 [24] and dominates the overall MR. From the angular de-
 168 pendences of the MR, we can distinguish between this
 169 effect and AMR [23].

170 Importantly, the switching fields in the R(H) loops
 171 do not change significantly during the thinning of the
 172 nanocontact, confirming that the magnetic states are fun-
 173 damentally identical in both conduction regimes. As de-
 174 pinning fields usually depend strongly on the geometry
 175 and size of the constriction, a constant switching field
 176 indicates that the transition from the state with a DW
 177 to the one without does not occur by depinning of the
 178 wall. Instead, a reverse domain nucleates at one of the
 179 two ends of the half ring, which then annihilates the DW
 180 at the constriction. In contrast to previous studies (e.g.
 181 Refs. [6–8, 24–26]), here the magnetization of the arms
 182 can be switched in low fields, independently of the precise
 183 geometry of the constriction, resulting in distinct stable
 184 configurations that can be probed at zero field. This
 185 means that we can uniquely identify the presence of a

186 DW and the resulting impact on the MR even at zero
 187 field, as depicted in Fig. 2(c).

188 It was shown previously that magnetostriction artifacts
 189 can lead to arbitrarily high MR values in applied fields
 190 [11–13]. In contrast to most other studies, our nanocon-
 191 tacts are rigidly attached to the substrate and atomic
 192 force microscopy (AFM) as well as SEM imaging do not
 193 reveal significant suspended parts of the contacts. In
 194 addition, permalloy is known to exhibit extremely low
 195 magnetostriction leading to fm maximum length changes,
 196 which do not lead to significant resistance changes [see
 197 Fig. 3(d) in Ref. 18]. We therefore do not expect signif-
 198 icant effects from magnetostriction. To completely rule
 199 out magnetostriction due to externally applied fields and
 200 to gauge the applicability of the effect for non-volatile
 201 devices, we compare the MR values at *zero* applied field:
 202 we obtain two distinct resistance levels with an MR ra-
 203 tio of up to 50% (see for example Fig. 2(c)). Further-
 204 more, apart from the switching event, the resistance lev-
 205 els do not change significantly when a field is applied
 206 (2(b),(c)). For example, we do not observe any change
 207 in the resistance for fields above 70 mT indicating that
 208 magnetostriction-related effects do not significantly con-
 209 tribute to the observed resistance change.

210 At the same time, we do not observe a significant sig-
 211 nature of tunneling transport (non-linear I-V character-
 212 istics or negative dR/dV [7]) in the interesting resistance
 213 range of about 10–30 k Ω . On the assumption that TMR
 214 in nanoscale contacts remains comparable to TMR in
 215 macroscopic vacuum tunnel junctions, the contribution
 216 to the MR effect due to tunneling transport was found
 217 to be small – even for contacts with resistance values
 218 beyond 30 k Ω (see supplemental material [23]). This im-
 219 plies that the conductance and the MR effects in the
 220 contacts considered here are dominated by ballistic trans-
 221 port effects. Hence, tunneling magnetoresistance (TMR)
 222 as well as tunneling AMR (TAMR [27]) can be excluded
 223 as the dominating effect in our experiments. In agree-
 224 ment with Ref. 24, our data show that we can also ex-
 225 clude AMR since neither the angle-dependence nor the
 226 sign of the MR signal in our $R(\alpha)$ measurements agrees
 227 with the characteristics of large AMR as sometimes ob-
 228 served in nanocontacts at very low temperature [27, 28].
 229 Anisotropic MR effects are therefore assumed to be neg-
 230 ligibly small in our nanocontacts (see supplemental ma-
 231 terial [23]).

232 Ultimately, this indicates that it is the presence of a
 233 narrow DW in the ballistic transport regime that leads
 234 to this large MR. We can therefore conclude that we un-
 235 ambiguously observe DWMR. Given the atomic size of
 236 the constriction in this resistance regime, it is the spin
 237 structure of the atoms at the very center of the contact,
 238 where the DW is located, that gives rise to the significant
 239 resistance changes observed. We have also studied pure
 240 Ni and Co contacts where we find similar results, indi-
 241 cating that the concurrent presence of Fe and Ni atoms

242 in Py is not responsible for the observed effects.

243 Numerous models treat DWMR in the diffusive limit
244 [4, 5, 29–32] but few have considered the ballistic con-
245 duction regime. The reduced dimensions of such contacts
246 require a self-consistent calculation of both the magnetic
247 as well as the electronic structure of the nanocontact.
248 Recent detailed ab initio calculations of this kind by Cz-
249 erner et al. [33] yield DWMR values of around 50% in
250 line with our experimental observation. Jacob et al. [3]
251 conclude that realistic MR values in Ni nanocontacts are
252 of the order of 30%, similar to what we observe.

253 A key observation in our experiments is the occurrence
254 of a sign change in the MR for a number of contacts in
255 the ballistic regime (see Fig. 2(a)). This sign change is
256 in contrast to previous experimental observations where
257 such behavior was only found in the diffusive and in the
258 tunneling regime [7]. Fig. 3 shows the quasi-static MR
259 for two consecutive resistance states of a nanocontact:
260 While the resistance changes from 12 k Ω to 9.5 k Ω , the
261 MR jumps from -4% to $+3\%$. The corresponding R(H)
262 loops (shown as insets) also show this behavior. Despite
263 this change in resistance, likely caused by a small atomic
264 reconfiguration at the narrowest part of the contact, the
265 switching fields between the P and AP states remain at
266 the same field values, allowing us to identify the magne-
267 tization configurations as explained above. Furthermore,
268 the simultaneous occurrence of a resistance change and
269 a sign change of the MR points to the same origin of the
270 two effects.

271 We therefore conclude that the underlying MR asso-
272 ciated with the presence of a DW depends on the pre-
273 cise atomic configuration of the constriction. Theoretical
274 approaches that are limited to simple geometries of the
275 constriction, such as single-atomic wires, cannot satisfy-

276 ingly describe this situation. Very recently Achilles et al.
277 [18] have considered different atomic configurations with
278 resistance values similar to the ones observed in our ex-
279 periments. Based on spin-dependent density functional
280 theory, the MR is evaluated as the difference in resistance
281 taken with and without a DW. Some of the atomic con-
282 figurations considered differ only by the position of one
283 or a few atoms. Precisely such atomic rearrangements
284 can be induced by thermal activation, for instance during
285 electromigration. In Ref. 18 the authors predict that, de-
286 pending on the chosen configuration, the MR can be posi-
287 tive or negative with a strongly varying magnitude. This
288 surprising result (in line with our observation) can be
289 understood based on symmetry considerations: It is shown
290 that a reduction of the symmetry of the nanocontact
291 drastically reduces the conduction through the majority
292 channel in the P state $g_P^{\uparrow\uparrow}$. In contrast to that, $g_P^{\downarrow\downarrow}$ and
293 the conduction values in the AP state $g_{AP}^{\uparrow\downarrow/\downarrow\uparrow}$ are much
294 less affected. Depending on the specific symmetries of the
295 contact, this behavior is shown to cause $g_{AP} > g_P$ (neg-
296 ative MR) or $g_{AP} < g_P$ (positive MR). This result cor-
297 roborates the hypothesis that small changes in the con-
298 figuration of the nanocontact, observed as changes in the
299 measured resistance, lead to pronounced changes in the
300 MR including sign changes. Ultimately, this agreement
301 between theory and experiment suggests that we can at-
302 tribute the large MR changes to spin-dependent trans-
303 port through discrete conductance channels that change
304 their transmission depending on the atomic arrangement
305 and the magnetic configuration of the narrowest part of
306 the nanocontact.

307 In summary, we have found a large DWMR (up to
308 50%) with both positive and negative sign at zero applied
309 field in electromigrated Py nanocontacts in the ballistic
310 transport regime. Our sample design and measurement
311 scheme allow us to control the spin structure at the con-
312 striction. At the same time we are able to minimize ar-
313 tifacts due to field-induced magnetostriction and impuri-
314 ties, as our thorough analysis of possible artifacts shows.
315 For the first time in the ballistic conduction regime, we
316 demonstrate that the reproducible resistance states ob-
317 served at zero applied magnetic field are associated with
318 two stable magnetic configurations, with and without a
319 DW pinned at the nanocontact. Our comparison of the
320 measured MR behavior with available theoretical models
321 shows that our results can only be reproduced by mod-
322 els that take into account spin polarized transport ef-
323 fects as well as the spatial and magnetic configuration
324 of the atoms at the narrowest part of the nanocontact.
325 Small changes in the atomic configuration, which appear
326 as abrupt changes in the resistance, lead to a large change
327 of the magnitude and even the sign of the MR that we
328 observe. This means that both the sign and magnitude of
329 the DWMR are governed by the precise geometrical ar-
330 rangement of the constriction on the atomic scale, which

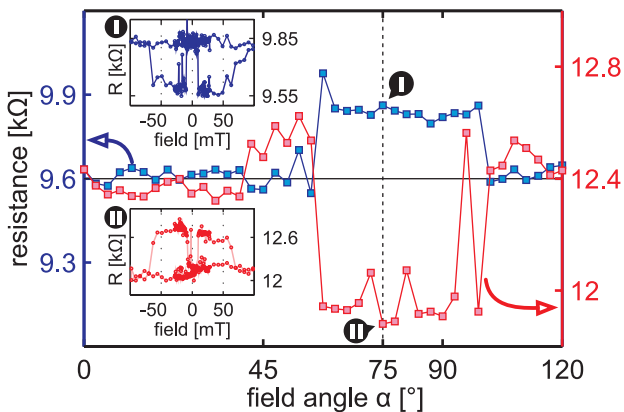


FIG. 3. (Color online) Resistance of a nanocontact as a function of field angle α after applying a magnetic field and relaxing it to zero along α . The data was obtained for two consecutive resistance states of a nanocontact (blue and red), indicating a change in the sign of MR associated with a change in contact resistance. Insets: R(H) major loops measured at $\alpha = 75^\circ$ obtained for the same contact configurations.

331 so far has mostly been neglected.

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