

## Evidence for phonon skew scattering in the spin Hall effect of platinum

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We measure and analyze the effective spin Hall angle of platinum in the low-residual resistivity regime by second-harmonic measurements of the spin-orbit torques for a multilayer of Pt|Co|AlO<sub>x</sub>. An angular-dependent study of the torques allows us to extract the effective spin Hall angle responsible for the dampinglike torque in the system. We observe a strikingly nonmonotonic and reproducible temperature dependence of the torques. This behavior is compatible with recent theoretical predictions which include both intrinsic and extrinsic (impurities and phonons) contributions to the spin Hall effect at finite temperatures.

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The demand for high-density and efficient data storage devices has driven the research on magnetic memories. Proposals were mainly based on using spin transfer torques for domain wall motion and magnetization switching [1]. However, spin transfer torque-based devices are plagued by the requirement of high writing current densities which result in deterioration of the material layers and hence limit the device life. A recent demonstration [2] of highly efficient current-induced switching via spin-orbit torques (SOTs) shows promising results that can overcome these limitations [1]. Such devices are made from magnetic multilayers which consist of a few monolayers-thick ferromagnetic (FM) material sandwiched between a normal metal (NM) and an oxide layer.

The injection of an in-plane current through the normal metal has been shown to efficiently manipulate the magnetization [3]. The torques have been attributed to the spin Hall effect (SHE) [3–6] arising from the charge to spin current conversion in the NM and the inverse spin galvanic effect (ISGE) [7–13] arising at the interfaces with the FM.

First, a charge current in the NM underlayer generates via the SHE a spin current flowing towards the FM layer. These spins enter the FM and exert by *s-d* exchange a dampinglike torque on the FM magnetization [2–4,14]. Second, due to inversion symmetry breaking at the NM|FM interface, the same charge current gives also rise to an (interfacial) nonequilibrium spin polarization via the ISGE [10,11,15]. Such spin polarization results in a fieldlike torque affecting the FM magnetization. It has actually been discussed how the

SHE and the ISGE can *individually* in principle generate both dampinglike and fieldlike torques due to subtler interfacial spin-orbit effects [16,17]. Indeed, we will argue later that in our system the SHE is dominating and responsible for both torques. Irrespective of their origin, whether SHE or ISGE, each torque can be described in terms of the corresponding component of an overall current-induced spin-orbit field acting on the magnetization: a longitudinal component  $\mu_0 H_{DL} \sim \hat{\sigma} \times \hat{m}$ , exerting a dampinglike torque  $\sim \hat{m} \times (\hat{\sigma} \times \hat{m})$ , and a transversal one  $\mu_0 H_{FL} \sim \hat{\sigma}$ , giving rise to a fieldlike torque of  $\sim \hat{m} \times \hat{\sigma}$ . Here  $\hat{m}$  is the magnetization direction, and  $\hat{\sigma}$  is that of the spin of the (nonequilibrium) SHE and/or ISGE electrons. In our experimental configuration the charge current flows along  $\hat{x}$ , whereas  $\hat{m} = \hat{z}$ ,  $\hat{\sigma} = \hat{y}$ , see Fig. 1.

Efficient magnetization switching using SOTs has motivated studies of various heavy metals so as to find materials with the highest spin Hall angle (SHA). The SHA characterizes the efficiency of charge-to-spin conversion and is defined as  $\theta_{sH} = \sigma_{sH}/\sigma = -\rho_{sH}/\rho$  with  $\sigma(\rho)$  and  $\sigma_{sH}(\rho_{sH})$ , respectively, as the charge and spin Hall conductivities (resistivities). There are various mechanisms giving rise to the SHE: extrinsic (side jump [18] and skew scattering [19,20]) and Berry curvature-induced intrinsic ones [21]. In metallic paramagnets it is difficult to identify materials where only one mechanism is at work. It is important to rather understand the dominant mechanism in a particular system in order to optimize it for possible technological applications. Indeed, phonon skew scattering has been recently suggested to play an important role at room temperature [22], and a thorough experimental study of its influence on the SHE is still lacking.

In this Rapid Communication we provide such a study by monitoring the temperature dependence of the SOTs ascribed to the SHE in low-residual resistivity Pt (5.3, 6.3  $\mu\Omega$  cm). Although the observed nonmonotonic behavior is unexpected

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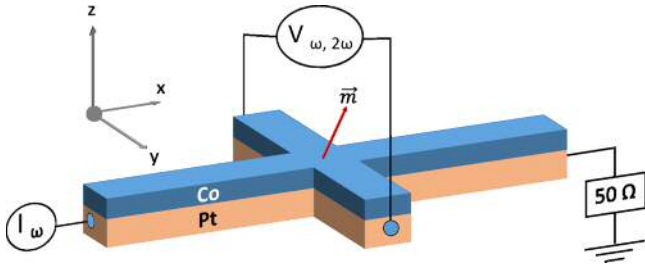


FIG. 1. Schematics of the second-harmonic measurement setup. A charge current is injected along  $\hat{x}$ , generating dampinglike and fieldlike effective spin-orbit fields which torque the magnetization  $\hat{m}$ . The dampinglike torque acts along  $\hat{\sigma} \times \hat{m}$ , and the fieldlike one acts along  $\hat{\sigma}$ . Here  $\hat{\sigma}$  is the direction of the current-induced nonequilibrium spin current (SHE) and density (ISGE).

83 and cannot be explained following the established phenomeno-  
84 logical analysis [23,24], it is compatible with the tempera-  
85 ture scaling derived from the microscopic theory [22]. The  
86 importance of “ultraclean” samples is further supported by  
87 the simpler monotonic behavior observed in high-residual  
88 resistivity Ta.

89 *Sample characterization.* First, we measure the evolution of  
90 the magnetic properties with temperature since the ferromag-  
91 netic layers in these stacks are only a few monolayers thick.  
92 The temperature dependence of the saturation magnetization  
93 in this thin-film structure is measured using superconducting  
94 quantum interference device magnetometry. This is plotted  
95 in Fig. 2, and in the relevant temperature range a constant  
96 value is found. The temperature dependence of the effective  
97 anisotropy is studied by measuring the extraordinary Hall  
98 voltage in individual Hall crosses during the application of  
99 a rotating magnetic field [25]. This angle-dependent variation  
100 of Hall voltage (seen in the inset of Fig. 2) when interpreted in  
101 terms of the Stoner-Wolfarth model [26] allows us to determine  
102 the anisotropy field and hence the effective anisotropy. The  
103 effective anisotropy constant is plotted in Fig. 2 and shows  
104 no significant variation. These measurements establish that the  
105 multilayer has a Curie temperature much larger than 300 K with  
106 no significant changes in magnetic properties in the considered  
107 temperature range.

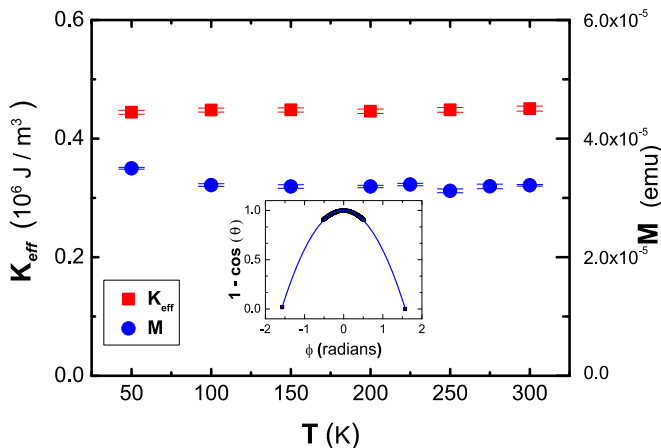


FIG. 2. Temperature dependence of  $K_{\text{eff}}$  and  $M$ .

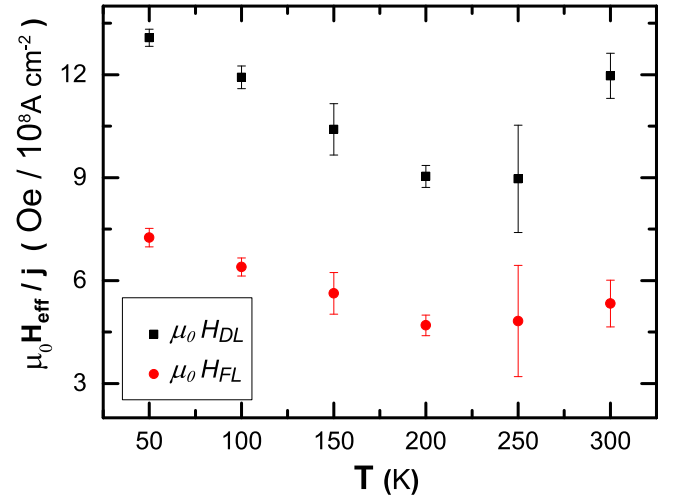


FIG. 3. Temperature dependence of the efficiency of dampinglike ( $\mu_0 H_{DL}$ ) and fieldlike ( $\mu_0 H_{FL}$ ) effective fields.

*Spin-orbit torque measurements.* Next, we perform spin-orbit torque measurements using the second-harmonics ( $2\omega$ ) technique [4,14,27] on patterned Hall bars. The material stack that is used (see the Supplemental Material [28]) is as follows: Pt(4.0)|Co(0.8,1.3)|AlO<sub>x</sub>(2.0) (all thicknesses in nanometers).

The  $2\omega$  measurements [4,14,27] are performed (see the Supplemental Material [28]) by injecting a low-frequency ( $\omega/2\pi = 13.7$ -Hz) sinusoidal ac signal through the nanowire (the  $x$  axis) while the sample is in a saturated magnetization state (the  $z$  axis). The effective fields are measured as a function of temperature, and this is shown in Fig. 3. We see a clear nonmonotonic dependence that is distinct from the temperature dependence of the magnetic properties shown in Fig. 2.

The observed temperature dependence of the spin-orbit torques can have various origins, such as: change in magnetic properties, spin-mixing conductance, the SHE, and the ISGE. We individually evaluate all these parameters to pinpoint the origin of the variation of the spin-orbit torques with temperature. First, as already shown, the magnetic properties of our sample are effectively temperature independent [see Fig. 2]. Second, experimental results [29] show that the spin-mixing conductance at the Pt|Co interface is largely temperature independent as well. We thus attribute any nonmonotonic change in the current-induced effective fields to a variation of the SHE and/or ISGE and the resulting torques exerted.

At this point we make a crucial observation, namely, that damping- and fieldlike terms change in unison, indicating a common origin for the two torques. This agrees with our previous conclusions [30] of the SHE being the likely cause for both SOTs in Pt|Co|AlO<sub>x</sub> as well as with results where the SHE was claimed to be the dominant effect for the dampinglike torque in this system [2,3,31]. As mentioned earlier, the generation of both torques via the SHE is due to interfacial spin-orbit effects [17]: Roughly, part of a  $\hat{\sigma}$ -polarized spin Hall current  $J_{sH}$  incoming on the Co layer is lost and turned into a  $\hat{\sigma}'$ -polarized spin current  $\delta J_{sH}$  by interfacial spin-orbit coupling. Once in the FM, the (remaining)  $J_{sH}$  and  $\delta J_{sH}$  exert dampinglike and fieldlike torques, respectively, on the

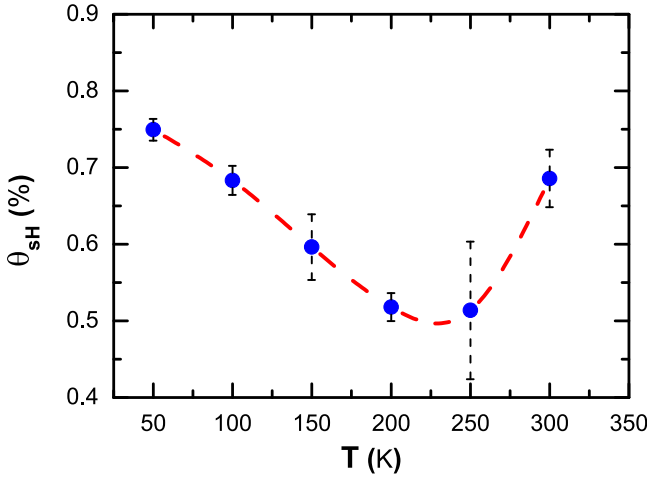


FIG. 4. Temperature dependence of the deduced spin Hall angle (blue dots — connected by a basis spline as a guide to the eye) derived from the dampinglike effective field. Practically identical behavior is found in the control sample, see Fig. S4 in the Supplemental Material [28].

147 magnetization. Since we cannot quantify the loss  $\delta J_{sH}$ , we  
 148 define an *effective* spin Hall angle assuming that the remaining  
 149 spin Hall flux is fully transmitted from Pt to Co [2,31–33],

$$\theta_{sH} = \frac{2\mu_0 H_{DLE} M_s t_{FM}}{\hbar j_e}, \quad (1)$$

150 where  $M_s$  is the saturation magnetization,  $t_{FM}$  is the ferro-  
 151 magnetic layer thickness, and  $j_e$  is the injected charge current.  
 152 We plot in Fig. 4 the temperature evolution of the calculated  
 153 effective spin Hall angle of Pt.

154 *Theoretical analysis and discussion.* We see in Fig. 4 that the  
 155 effective SHA varies nonmonotonically with temperature. We  
 156 also observe that there is a significant upturn in its magnitude  
 157 around 240–250 K. This is a distinct temperature in this system  
 158 as the spin Hall source in our system Pt is known [34] to have  
 159 a Debye temperature of  $T_D = 240$  K. The Debye temperature  
 160  $T_D$  gives an estimate of the temperature beyond which all  
 161 phonon modes are excited and behave classically.

162 The temperature dependence of the SHA provides us with  
 163 the opportunity to gain insight into the relative magnitude of the  
 164 different mechanisms responsible for the SHE in the system.  
 165 We will start by considering both intrinsic and extrinsic (skew  
 166 scattering) mechanisms: The importance of the former in  $4d$   
 167 and  $5d$  transition metals is known [35] and so is the fact that  
 168 in low-impurity samples the dominant extrinsic contribution  
 169 comes from skew scattering [6,24,36–39].

170 We now analyze the temperature dependence of the SHA  
 171 [24,40] based on the scaling suggested by Tian *et al.* [23] and  
 172 the Supplemental Material [28]. The starting point is

$$\rho_{sH} \approx -(\sigma_{sH}^{\text{int}} + \sigma_{sH}^{\text{ss}})\rho^2 \approx -\sigma_{sH}^{\text{int}}\rho^2 + \rho_{sH}^{\text{ss}}, \quad (2)$$

173 having assumed that skew scattering ( $\sigma_{sH}^{\text{ss}}$ ) and intrinsic ( $\sigma_{sH}^{\text{int}}$ )  
 174 contributions act as parallel channels  $\sigma_{sH} = \sigma_{sH}^{\text{int}} + \sigma_{sH}^{\text{ss}}$  and  
 175 that  $\sigma \gg \sigma_{sH}$ . The latter condition implies  $\sigma_{sH} \approx \rho_{sH}/\rho^2$  with  
 176  $\rho$  as the longitudinal resistance of the Pt layer and was used in  
 177 the second passage above. Then it is argued that the skew scatter-  
 178 ing resistivity scales as  $\rho_{sH}^{\text{ss}} = \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}} + \theta_{sH}^{\text{ss,phon}} \rho^{\text{phon}}$

with the spin Hall angle due to phonon skew scattering being  
 temperature *independent*, whereas  $\rho^{\text{imp}}$  ( $\rho^{\text{phon}}$ ) represents the  
 resistivity from impurities (phonons). The split  $\rho = \rho^{\text{imp}} +$   
 $\rho^{\text{phon}}$  follows Matthiessen's rule. One thus has

$$\rho_{sH} \approx -\sigma_{sH}^{\text{int}}\rho^2 + \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}} + \theta_{sH}^{\text{ss,phon}}(\rho - \rho^{\text{imp}}). \quad (3)$$

In the lowest-order approximation phonon skew scattering,  
 i.e., the last term on the right-hand side of Eq. (3), is neglected,  
 and  $-\rho_{sH}$  can be plotted vs  $\rho^2$ . In this regime, the slope of  
 the linear relation between  $\rho_{sH}$  and  $\rho^2$  describes the intrinsic  
 contribution to the SHE, indicating the sign of the SHA of  
 the material. If this analysis yields inconsistent results, the last  
 term in Eq. (3) is also taken into account [24]. In our case,  
 however, even the full expression (3) is not enough since the  
 relation between  $\rho_{sH}$  and  $\rho$  is nonmonotonic, see Figs. S5 and  
 S6 of the Supplemental Material [28].

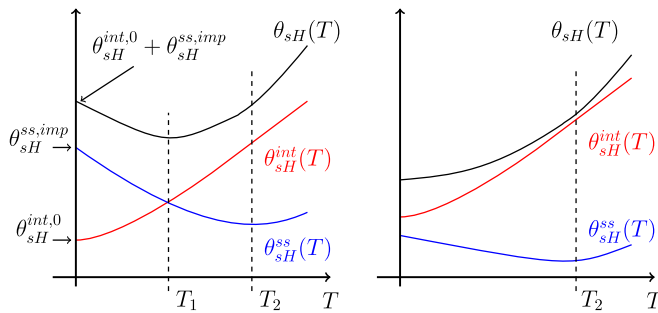
This suggests the need to revisit the established temperature  
 scaling relation assumed for the SHA. The microscopic theory  
 of phonon skew scattering shows indeed that the corresponding  
 SHA is not temperature independent but rather a function of the  
 temperature  $\theta_{sH}^{\text{ss,phon}} \rightarrow \theta_{sH}^{\text{ss,phon}}(T)$ . As a consequence Eq. (3)  
 is modified to

$$\rho_{sH} \approx -\sigma_{sH}^{\text{int}}\rho^2 + \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}} + \theta_{sH}^{\text{ss,phon}}(T)(\rho - \rho^{\text{imp}}). \quad (4)$$

The phononic part of the SHA  $\theta_{sH}^{\text{ss,phon}}$  increases linearly  
 with  $T$  at high temperatures ( $T \gtrsim T_D$ ), whereas, clearly, it has  
 to vanish at low temperatures, although its precise behavior at  
 $T < T_D$  is not yet known [41]. Its asymptotics can however be  
 used to determine the qualitative behavior of the full SHA in the  
 whole temperature range. An order-of-magnitude estimate for  
 a metallic system yields  $\sigma_{sH}^{T_D}/\sigma_{sH}^0 \lesssim 10^{-1}$  with  $\sigma_{sH}^{T_D}$  ( $\sigma_{sH}^0$ ) as  
 the spin Hall conductivity at the Debye (zero) temperature [22].  
 Coupled with the moderate change in the charge conductivity  
 over the same temperature range of  $\sigma^{T_D}/\sigma^0 \lesssim 1$ , see Fig. S7 of  
 the Supplemental Material [28], one has  $\theta_{sH}^{\text{ss,phon}}(T \approx T_D) <$   
 $\theta_{sH}^{\text{ss,imp}}$ . The resulting qualitative behavior shown in Fig. 5 is  
 compatible with the measurements in clean Pt samples. In a  
 clean system the low- $T$  SHE is dominated by skew scattering,  
 i.e.,  $-\sigma_{sH}^{\text{int}}\rho^2(T \rightarrow 0) < \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}}$ . Thus, the SHA should  
 eventually decrease in magnitude from  $T = 0$  down to a min-  
 imum at a temperature  $T_1$  given by  $-\sigma_{sH}^{\text{int}}\rho^2(T_1) \approx \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}}$   
 and increase afterwards. Furthermore, at a higher temperature  
 of  $T_2 \gtrsim T_D$  such that  $\theta_{sH}^{\text{ss,phon}}(T_2)[\rho(T_2) - \rho^{\text{imp}}] \approx \theta_{sH}^{\text{ss,imp}} \rho^{\text{imp}}$   
 phonon skew scattering would start dominating impurity skew  
 scattering, yielding an asymptotic linear behavior,

$$\theta_{sH}(T \gtrsim T_2) \sim [\sigma_{sH}^{\text{int}} + \sigma_{sH}^{\text{ss},T_D}]T, \quad (5)$$

with  $\sigma_{sH}^{\text{ss},T_D}$  as the saturation value for the phonon skew scatter-  
 ing spin Hall conductivity at  $T \gtrsim T_D$  [22]. A few comments  
 are in order: (i) The qualitative analysis yields  $T_1 \lesssim T_D \lesssim T_2$ ,  
 but we cannot give quantitative estimates of the temperatures  
 $T_1, T_2$ . These require precise knowledge of various system  
 parameters, notably electron-phonon and phonon-phonon cou-  
 pling strengths. (ii) The nonmonotonic behavior predicted  
 by Eq. (4) for clean samples does not require phonon skew  
 scattering to be stronger than impurity skew scattering, which  
 happens only at  $T > T_2$ : It is enough to recognize that the  
 phonon SHA is itself a function of the temperature  $\theta_{sH}^{\text{ss,phon}} =$



4 FIG. 5. Sketch of the temperature behavior of the SHA for an ultraclean sample (skew scattering dominated, left panel) and a dirty one (intrinsic dominated, right panel). The sketch is based on Eq. (4) and built from knowledge of the high- and low- $T$  asymptotics, which imply the existence (absence) of a minimum in clean (dirty) systems (see the Supplemental Material [28]). The precise behavior in the intermediate temperature range is however not yet known, nor can accurate values for  $T_1, T_2$  be given since both temperatures depend on various system parameters. An order-of-magnitude estimate for Pt yields  $T_1 \lesssim T_D \lesssim T_2$  and suggests that  $T_1$  should be higher the cleaner the sample. In dirty samples the compensation between intrinsic (red) and skew scattering (blue) curves can give rise to an effectively constant SHA over a broad  $T$  range as observed in Ta (for the details see Fig. S4 in the Supplemental Material [28]).

[28]) here. This is essentially because the intrinsic and extrinsic contributions scale differently [24] with the resistivity of the metal. It was recently shown [40] that tuning the conductivity of Pt leads to a transition of the SHE from a “moderately dirty” to a “superclean” regime. This corresponds to a transition from an intrinsic-dominated to an extrinsic-dominated regime. The intrinsic term scales with  $\propto \rho^2$  and in the low-resistivity limit is dominated by the phonon contribution, which scales roughly with  $\propto (\rho - \rho^{\text{imp}})$ . This could be the reason why other experimental investigations of the spin Hall angle of Pt with higher resistivity have observed the dominance of intrinsic contributions, whereas they have observed dominance of extrinsic contribution in the case of low resistivity Au [24].

To summarize, we used the second-harmonic technique to measure the spin-orbit torque in Pt|Co|AlO<sub>x</sub> and Ta|CoFeB|MgO.

We deduced the temperature-dependent evolution of the SHA of clean Pt and dirty Ta. The reproducible nonmonotonic behavior observed in Pt cannot be accounted for by standard phenomenology but is compatible with the temperature scaling derived from microscopic phonon skew scattering theory. The monotonic behavior observed in dirty Ta is instead ascribed to the weakness of skew scattering contributions. Our results reveal that extrinsic contribution to the SHE might be the key to understanding the temperature dependence in normal metals as well and thus provides a more comprehensive understanding of the spin Hall angle and the resulting spin-orbit torques in this system.

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231  $\theta_{sH}^{ss, \text{phon}}(T)$ , vanishing at  $T = 0$  and (linearly) increasing at high  
 232 temperatures. (iii) Although  $\theta_{sH}^{ss, \text{phon}}(T \rightarrow 0) = 0$  has to hold,  
 233 the approach to zero could be nontrivial and affected, e.g., by  
 234 the interplay between impurity and phonon scattering [42].

235 The picture changes in dirty systems with strong intrinsic  
 236 SHE such that  $-\sigma_{sH}^{\text{int}} \rho^2(T \rightarrow 0) > \theta_{sH}^{ss, \text{imp}} \rho^{\text{imp}}$ . In this case  
 237 Eq. (4) predicts a simpler monotonic behavior of the SHA, once  
 238 more compatible with our measurements in a dirty Ta sample  
 239 (137  $\mu\Omega$  cm), see Fig. S4 of the Supplemental Material [28].  
 240 Ta has a strong intrinsic SHE [2],  $T_D$  is comparable to that of  
 241 Pt [43], and our sample is 20 times as resistive as the Pt sample  
 242 used. We observe a considerably larger SHA with no minimum,  
 243 indeed roughly constant in the considered temperature range.

244 The SHA transition through the intrinsic and extrinsic  
 245 regimes can be expected due to the low residual resistivity of Pt  
 246 (5.3, 6.3  $\mu\Omega$  cm), as we find (see the Supplemental Material

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